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**COMPUTER CODES FOR  
THE EVALUATION OF SPACE RADIATION HAZARDS**

**VOL. 5 ELECTRON MONTE CARLO**

**D2-90418-5**

**Prepared for**

**NATIONAL AERONAUTICS AND SPACE ADMINISTRATION  
MANNED SPACECRAFT CENTER**

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## GENERAL INFORMATION

The Electron Monte Carlo Program was written for an IBM 7094 computer.

The program consists of a main input program and several subroutines written in FORTRAN and FAP programming languages.

### PURPOSE

The calculation of an electron flux penetrating a shield is complicated by scattering and straggling so that Monte Carlo techniques are necessary to achieve an acceptable solution. This Electron Monte Carlo program was developed specifically for the problem of space radiation shielding.

It is desirable to know, given the energy of electrons incident on a particular material or shield, how many of these electrons penetrate the shield and their energy after penetration, and also the energy deposition within the shield.

The damage to objects behind the shield can then be determined. The thickness of a particular shield necessary to protect instruments or humans can also be determined.

The shield is considered to consist of infinite parallel slabs. Its geometry (thickness) and the material composition are inputs to the program. The source of electrons incident on the shield face is described by the initial energy of the electrons and their angle of incidence. The electrons penetrate the shield in finite increment thicknesses that are determined by the user. The electrons then suffer discrete energy losses and angular deflections at the end of each increment.

This process is continued until the electrons are transmitted or their energy goes below the energy cut-off.

The results of the penetration calculations are expressed in the energy spectrum and the angular distribution of the transmitted radiation. Also, the spatial distribution of energy loss due to radiation loss in the shield is expressed in the output.

### ASSUMPTIONS

Monte Carlo analysis of the individual collisions suffered by an electron penetrating a shield is prohibitive since many thousands of collisions are made by each electron. Therefore, the electrons were allowed to penetrate a series of small increments of thickness. The electron is assumed to have suffered a discrete energy loss and angular deflection at the end of each increment.

It is also assumed that when an electron passes from one material to another in an increment, the collision point is considered to be at the material interface and the next increment originates from that point.

### LIMITATIONS

A monoenergetic source must be used. The angular distribution of the source can be monodirectional or isotropic.

The shield is limited to twelve successive slabs. A slab can consist of any material for which range and ionization energy loss data is available (see Ref. 1). Each slab can be divided into a maximum of 15 regions for the radiation energy loss

spatial distribution. A shield can have as many as 20 transmission boundaries for forward transmission distribution information. The backscatter transmissions are valid only for the total thickness of the shield. There can be up to 15 energy divisions and 16 angle divisions for the transmission distribution and 15 energy divisions for the radiation loss distribution.

#### RECOMMENDATIONS

At present, only a monoenergetic source is available in the program. However, there does exist an option for another source energy spectrum such as a fission electron distribution.

Also, only a spatial distribution for radiation energy losses is recorded. A distribution of all energy losses in the shield can be obtained with only minor changes to the program.

## PROCEDURE

### NOMENCLATURE

A list of symbols and the corresponding names used in the program are presented in Table 1.

### METHOD

In the Monte Carlo method, each particle is followed from its source to its end, i.e., transmission or energy degradation below the cut-off energy. The results of many such particle histories are recorded and these results represent the physical situation.

The calculational scheme was based on the method of Leiss, Penner, and Robinson (Ref. 2), which was also employed by Perkins (Ref. 3). The initial energy,  $E_0$ , of an electron from a monoenergetic source is specified in the input. The angle of incidence,  $\theta_0$ , measured with respect to the shield normal, is either monodirectional and is specified in the input, or is determined from an isotropic distribution. In the latter option,  $\cos \theta_0 = R$ , where  $R$  is a random number from 0 to 1. This then gives an angle of incidence between 0 and  $90^\circ$ .

The electron is started at the face of the shield where  $ZT = 0$  and its total penetration is measured in the z-direction along the shield normal.

The distance the electron moves in the direction of  $\theta$  to its next collision point is chosen in either of two ways:  $\Delta T = C$ , a constant increment; or  $\Delta T = C/E$ . The choice is optional to the user. The total penetration of the

TABLE I. Nomenclature

MATH SYMBOL	PROGRAM SYMBOL	DEFINITION	UNITS
$E_0$	EINT	Initial source energy of electron	Mev
$\theta_0$	THINT	Angle of incidence of source electrons	Degrees
R	RAND	Random number	
E	ENERGY	Energy of electron at a collision point	Mev
$\theta$	THETA	Angle of electron direction measured with respect to shield normal	Radians
$\cos \theta$	COSINE	Cosine of THETA	Radians
$\theta_{\text{scat}}$	THTSCT	Scatter angle of electron measured with respect to previous direction	
$\Delta t$	DELT	Path length of electron from one collision point to the next	gm/cm <sup>2</sup>
t	T	Used in radiation energy loss calculation	
	TEST	Path length of electron measured along shield normal	gm/cm <sup>2</sup>
ZT	TTOT	Total penetration of electron measured along shield normal	gm/cm <sup>2</sup>
	NOSLAB	Number of slabs in the shield	
	NI	Number of boundaries for which transmission distributions are desired	
	TMAX(J)	Thickness of each slab J	gm/cm <sup>2</sup>

TABLE 1. Nomenclature (continued)

MATH SYMBOL	PROGRAM SYMBOL	DEFINITION	UNITS
j	J	Denoted slab the electron is in at the time of calculation	
ZB	SUM(J)	The right boundry of slab J	gm/cm <sup>2</sup>
	ISLB	Denotes the transmission boundary	
	ZB(ISLB)	Z coordinate of the transmission boundary	gm/cm <sup>2</sup>
	REGNO(J)	Number of subregions of each slab for recording radiation energy losses	
	IREG	Region in which radiation energy loss has occurred	
1/X <sub>o</sub>	XZRO	Inverse of radiation length	cm <sup>2</sup> /gm
A <sub>j</sub>	A(J)	Atomic weight of material of slab J	
Z <sub>j</sub>	Z(J)	Atomic number of material of slab J	
	REG(I, J)	Region boundaries for each slab J for recording radiation energy loss	gm/cm <sup>2</sup>
	KERROR	Error indicator	
E <sub>ion</sub>	EION	Ionization energy loss	Mev
E <sub>rad</sub>	ERAD	Radiation energy loss	Mev
dE/dx	DEXD	Rate of ionization energy loss	Mev cm <sup>2</sup> /gm

TABLE 1. Nomenclature (Continued)

MATH SYMBOL	PROGRAM SYMBOL	DEFINITION	UNIT
$\chi$	CHI	Angle in base of cone around previous electron direction used to determine new electron direction	
	RE	Range of electron of energy, E, gm/cm <sup>2</sup>	
	ECUT(J)	Energy cut-off for material of slab J	Mev
	NOHIST	Number of histories desired	
	IHIST	Number of histories being calculated	
$\int_0^y f(0) y dy$	FZINT(I)	Table of integral of function for $y = 0, 9.3$	
$y$	UPLIM(I)	Upper limit for table of integrals	
$\int_0^y \nu f^{(1)}(\nu) d\nu$	F1INT(I)	Table of integral of function for $y = 0, 9.3$	
$\int_0^y \nu^2 f^{(2)}(\nu) d\nu$	F2INT(I)	Table of integral of function for $y = 0, 9.3$	
	ARG(I)	Table of arguments for exponential integral table	
$E_1(\text{ARG})$	EI(I)	Table of exponential integrals	
$E_1(\ln E_0/E)$	EONE	Value of exponential integral for which the argument must be found	
	RAND1	Number used to start random number generator	

TABLE 1. Nomenclature (continued)

MATH SYMBOL	PROGRAM SYMBOL	DEFINITION	UNIT
B	BBIG	Parameter used in Moliere	
b	SSML or SMLB	Parameter used in Moliere	
	SLOPE	Slope of plot of equation, $B - \ln B = b$	
$B^2$	BETSQ	Used in Moliere	
	DEN	Normalizing integral	
	VALUE	Used in Moliere	
	RANGE(I, J)	Table of ranges for slab J and energy I	gm/cm <sup>2</sup>
	RATE(I, J)	Table of ionization rate for slab J and energy I	Mev cm <sup>2</sup> /gm
	E(I, J)	Table of energies for range and rate tables	Mev
	IRDL(I, J, K)	Radiation energy loss array for region I of slab J and energy K	
	NANT(I, J, K)	Number transmitted array for energy I, angle bin J and transmission boundary K	
	FNEE(I, J, K)	Energy transmission array for energy bin I, angle bin J, and transmission boundary K	
C	FACTOR	Input constant to control increment thickness	

new collision point is then  $ZT = \sum (\Delta T_i \cos \theta_i)$ . A test is now made to determine whether the electron has been: transmitted through either the front or the back face of the shield, scattered forward to the next slab, scattered backward to a previous slab, or remains in the same slab.

If transmission has occurred, the energy and angle,  $\theta$ , are recorded.

A new history is then begun.

If the electron has been scattered forward or backward to another slab, the slab counter,  $J$ , is adjusted by +1 or -1, respectively, and the collision point is considered to be at the boundary between the two slabs. The actual

$\Delta T$  the electron traveled is determined by  $\Delta T = \frac{ZT - Z}{\cos \theta}$ .

### Energy Losses

**IONIZATION ENERGY LOSS.** When a collision point has been established, the electron is scattered and some of its energy expended due to radiation energy loss and ionization energy loss. For ionization loss,

$\Delta E_{ion} = \frac{dE}{dx} \Delta T$ ,  $\frac{dE}{dx}$  is the average ionization energy loss for an electron of energy,  $E$ , for the material of slab,  $J$ .

**RADIATION ENERGY LOSS.** The radiation loss probability was obtained from the relationships derived by Bethe and Heitler (Ref. 4). The inverse of the radiation length,  $X_o^{-1}$ , for slab  $J$  is calculated as

$$\frac{1}{X_o} = \frac{4\pi N}{A_i} Z_i^2 r_o^2 \ln(183 Z_i^{-1/3}) \quad (1)$$

where  $\alpha = 1/137$ ,  $N = 6.02 \times 10^{23}$  is Avogadro's number, and  $r_o = 2.28 \times 10^{-13}$ .

The probability of an electron of energy,  $E_0$  degrading to an energy between  $E$

and  $E + dE$  by radiation loss is

$$P(E_0 - E) = \frac{1}{E_0} \frac{\ln \frac{E_0}{E}}{\Gamma(t/\ln 2)} \left[ (t/\ln 2) - 1 \right] \quad (2)$$

where  $t = \Delta T/X_o$ .

This function can be shown to be normalized, therefore,

$$R = \int_0^E \frac{1}{E_0} \frac{\ln \frac{E_0}{E}}{\Gamma(t/\ln 2)} dE \quad (3)$$

If  $t/\ln 2 \ll 1$ , and with proper substitutions,

$$R \sim \int_{\ln E_0/E}^{\infty} \frac{e^{-x}}{x} t/\ln 2 dx \quad (4)$$

$$R \sim t/\ln 2 E_1(\ln E_0/E)$$

where  $E_1$  is the exponential integral of the argument. The new energy,  $E$ , after radiation loss, is then determined from the above expression and the radiation energy loss,  $E_{rad} = E_0 - E$ .

Therefore, the new energy of the electron at the end of its path increment is found to be

$$E = E_0 - (E_{rad} + E_{ion}).$$

If the spatial distribution of radiation loss is desired, this radiation energy loss is tallied according to the energy division and region in which the loss occurred.

## Scatter Angle

The scatter angle of the electron is determined from the Moliere relationships discussed by Bethe (Ref. 5). The distribution function is expanded in a power series in  $1/B$  which gives,

$$f(\theta_{\text{scat}}) \theta_{\text{scat}} d\theta_{\text{scat}} = \gamma dy \left[ f^{(0)}(\gamma) + B^{-1} f^{(1)}(\gamma) + B^{-2} f^{(2)}(\gamma) + \dots \right] \quad (5)$$

where:  $f^{(0)}(\gamma) = 2\gamma e^{-\gamma}$ ,

$$f^{(1)}(\gamma) = 2e^{-\gamma} \left[ (\gamma^2 - 1) \left\{ E_i(\gamma)^2 - \ln \gamma^2 \right\} - 2(1 - 2e^{-\gamma}) \right]$$

$$\frac{1}{4} e^{-\gamma} f^{(2)}(\gamma) = \left[ \Psi^2(2) + \Psi^1(2) \right] (\gamma^4 - 4\gamma^2 + 2) + \int_0^1 t^{-3} dt \left[ \ln t/(1-t) - \Psi(2) \right]$$

$$\left[ (1-t)^2 e^{\gamma^2 t} - 1 - (\gamma^2 - 2)t - \left( \frac{1}{2} \gamma^4 - 2\gamma^2 + 1 \right) t^2 \right]$$

The average energy over the path increment used in the Moliere calculation is expressed as

$$E_{\text{mol}} = E - (E_{\text{rad}} + E_{\text{ion}})/2. \quad (6)$$

The variable  $b$  is determined as

$$b = \ln \left[ \frac{6680 \Delta T (Z_i + 1) Z_i^{1/3} z^2}{B^2 A_i (1 + 3.34 \alpha^2)} \right] \quad (7)$$

where  $z^2 = 1$ , is the square of the charge of the particle;  $B^2 = 1 - \left( \frac{.51}{E_{\text{mol}} + .51} \right)^2$ , and  $\alpha^2 = (Z_i/137B)^2$  is the deviation from the Born approximation.

The equation,  $B - \ln B = b$ , is solved for the expression  $B$ , using an iterative scheme.

The variable  $\gamma$  is defined by

$$\gamma = \theta_{\text{scat}} / (X_c B^{1/2}), \quad (8)$$

where  $\theta_{\text{scat}}$  is the scatter angle measured with respect to the previous electron direction.

The parameter,  $X_c$  defined as the total probability of a single scattering through an angle greater than  $X_c$  is exactly one, and

$$X_c^2 = \frac{4\pi N \Delta T e^4 Z (Z + 1) z^2}{A_i \beta_i^4 (E_{\text{mol}} + 0.51)^2} \quad (9)$$

where  $e = 4.8028 \times 10^{-10}$  esu.

Substituting,

$$f(\theta_{\text{scat}}) d\theta_{\text{scat}} = \frac{d\gamma}{X_c B^{1/2}} G(\gamma) \quad (10)$$

$$\text{where } G(\gamma) = f^{(0)}(\gamma) + B^{-1} f^{(1)}(\gamma) + B^{-2} f^{(2)}(\gamma)$$

Using direct Monte Carlo to determine the scatter angle from the above we have

$$R = \frac{\int_0^\gamma [G(\gamma)] d\gamma}{\int_0^{\pi/X_c B^{1/2}} [G(\gamma)] d\gamma} \quad (11)$$

To solve for  $\theta_{\text{scat}}$  the following process was used. The integrals of each of the functions,  $f^0$ ,  $f^1$ , and  $f^2$ , integrated from 0 to  $\gamma$ , were calculated separately and put in tables for  $\gamma$  in increments up to 9.3. These functions were integrated without their appropriate power of  $B$  since it is independent of  $\gamma$ . The upper limit of the denominator of Eq. (11) was determined and a table search

determined the values of the integrals of the three functions. These integrals were then multiplied by the power of B and the result yielded the value of the denominator of Eq. (11). This value was then multiplied by a random number which gave the value of the integral in the numerator of Eq. (11). Another table search, this time on the value of the integral, found the upper limit of the numerator. The scatter angle is then

$$\theta_{\text{scat}} = \sqrt{\frac{X}{c}} B^{1/2} \quad (12)$$

If the scatter angle is revolved around the previous electron direction, a right cone is formed. The intersection of the new electron direction and the base of the cone can be at any point on the circumference of the base of the cone. Therefore, an angle X is randomly chosen from 0 to  $2\pi$  to determine this point of intersection, i.e.,  $X = 2\pi R$  (see Fig. 1). From the geometry, the new direction,  $\theta$ , measured with respect to the shield normal is found from the expression:

$$\cos\theta_i = \cos\theta_{i-1} \cos\theta_{\text{scat}} + \cos X \sin\theta_{\text{scat}} \sin\theta_{i-1}$$

This concludes the calculations necessary for one collision. This process is repeated until the electron history is terminated by transmission or energy degradation below the cut-off energy. Then, when the requested number of histories have been completed, the energy and angular distributions for transmission and/or the spatial distribution of radiation energy losses are edited.

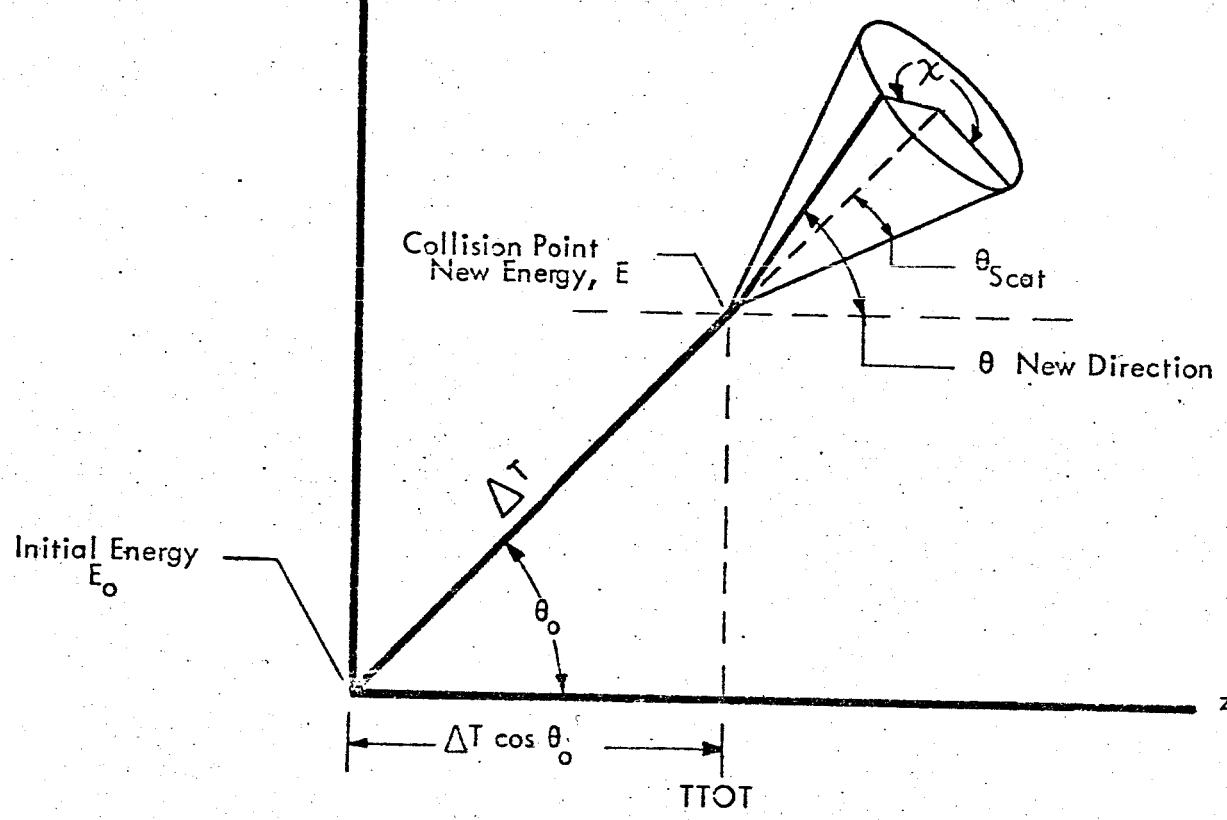


FIGURE 1. Geometry of Collisions

## RESULTS

The results of the Monte Carlo calculations were compared with existing experimental and theoretical data and found to be in good agreement. A comparison with Monte Carlo data of Perkins (Ref. 3) for 2 Mev electrons normally incident on an aluminum shield is shown in Fig. 2.

The extrapolated range of electrons from 1 to 8 Mev normally incident on an aluminum shield was compared with the analytic expression determined by Katz and Penfold (Ref. 6). Table 2 illustrates the comparison.

The backscatter electron results computed by the Monte Carlo program were compared to data obtained experimentally by Wright and Trump (Ref. 7).

Figure 3 shows this comparison.

An investigation of the effect of the increment thickness or  $\Delta T$  used in the calculation was made. Increments from .025 to .106 gm/cm<sup>2</sup> were used for a shield of aluminum. The results were found to lie within the statistical error associated with the number of histories processed and the number of electrons penetrating the slab (see Fig. 4). It was concluded that the Monte Carlo calculations are not limited by the choice of  $\Delta T$ .

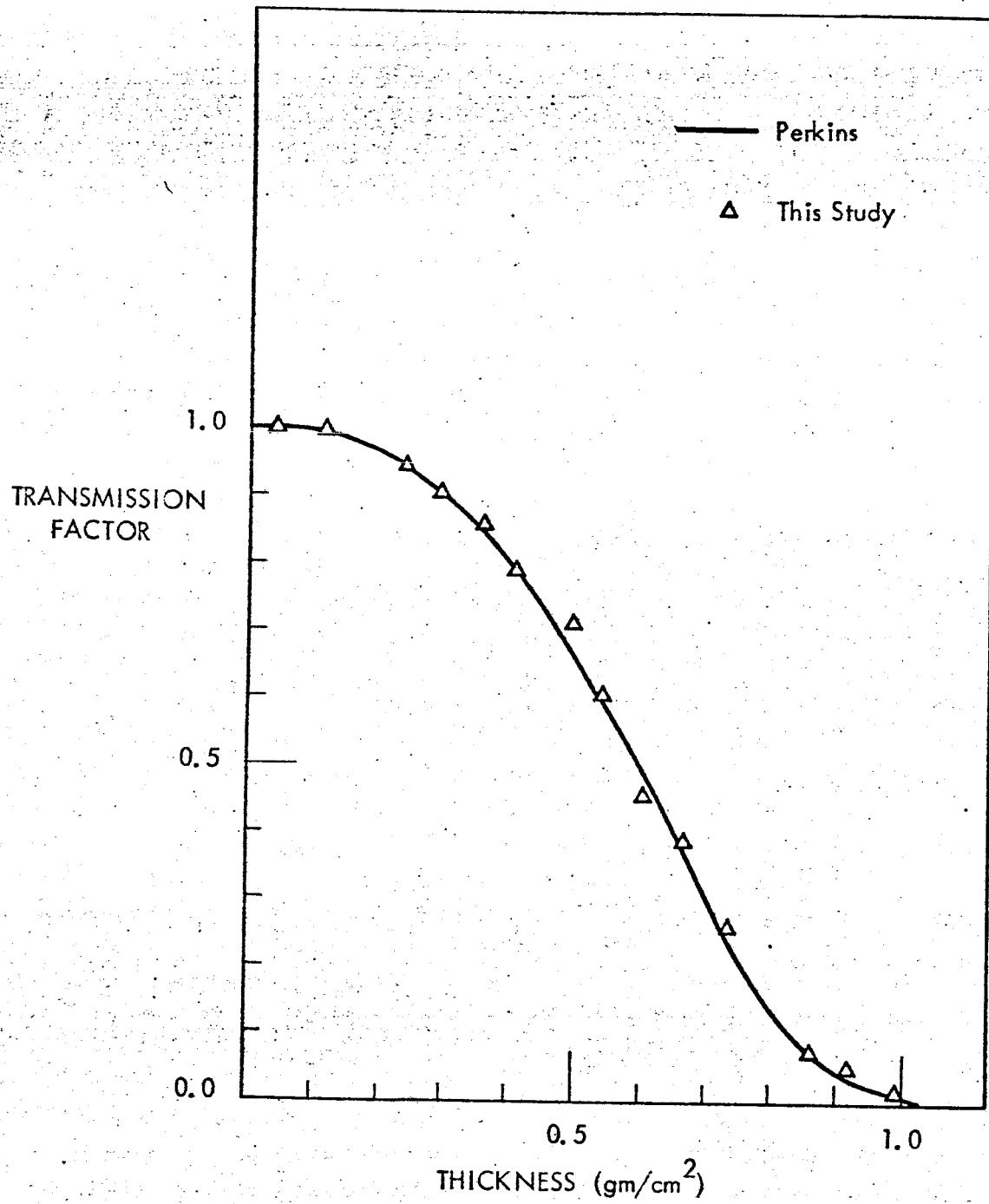


FIGURE 2. Comparison of Results of This Program With the Data of Perkins

TABLE 2. Comparison of the Results of this Program with that of Katz and Penfold

<u>E</u> (Mev)	<u>R (calc)</u> ( gm/cm <sup>2</sup> )	<u>R (ref. 6)</u> (gm/cm <sup>2</sup> )
1	0.41	0.42
2	0.98	1.05
3	1.50	1.48
4	2.00	2.01
6	3.10	3.07
8	4.10	4.13

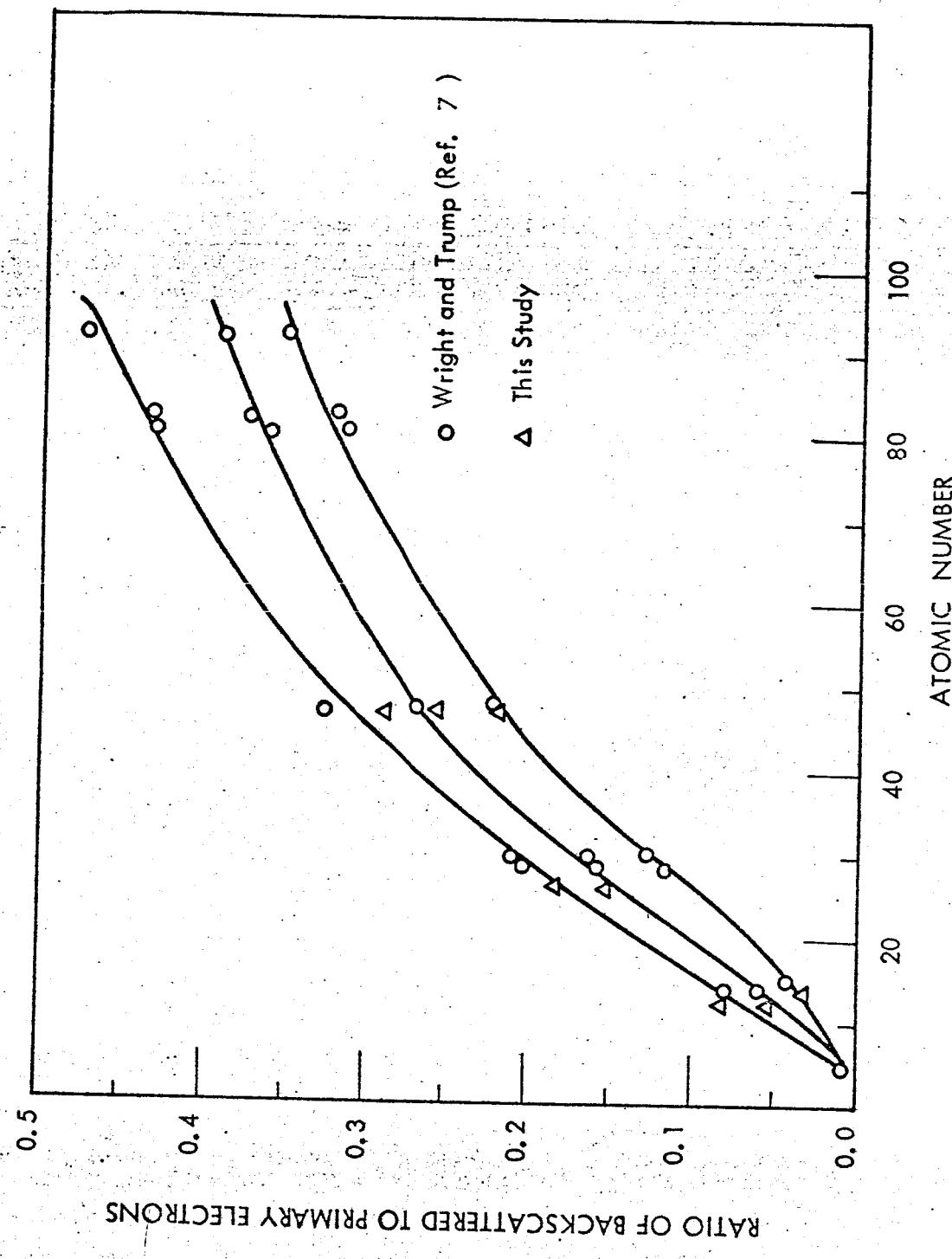


FIGURE 3. Comparison of the Results of This Program With the Data of Wright and Trump.

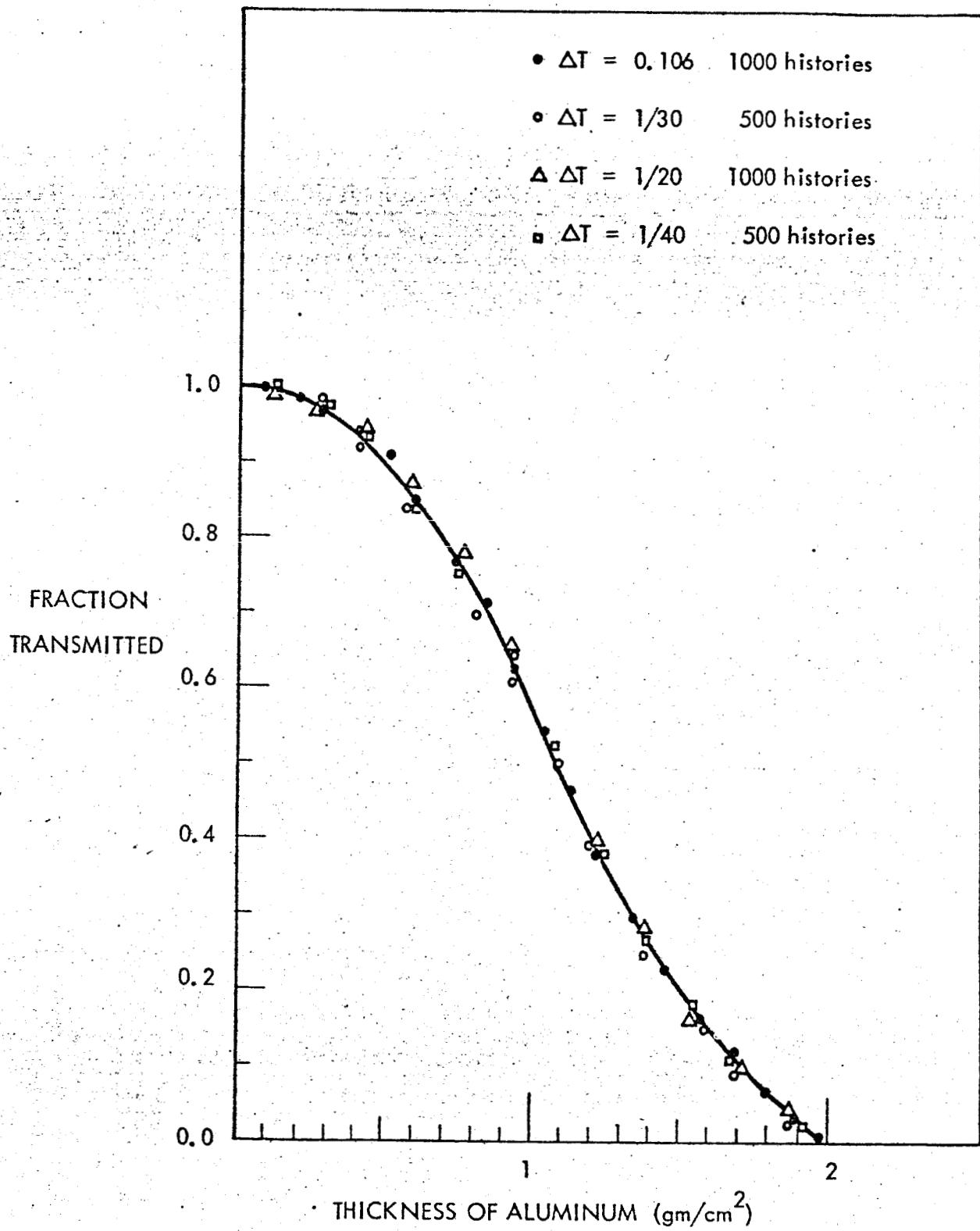


FIGURE 4. Comparison of Increments  $\Delta T$

## INPUT PREPARATION AND OUTPUT DESCRIPTION

### INPUT DATA PREPARATION

Following the data card will always be the two sets of permanent tables presented in Tables 3 and 4.

The following cards are necessary for each problem:

#### Card 1. Problem Description Card (Always Necessary)

<u>Column</u>	<u>Variable</u>	<u>Format</u>	<u>Definition</u>
1-72	DISCPT(I)	12A6	Any 72 characters for user to describe the problem. This will be written out at beginning of output.

#### Card 2. Option Card (Always Necessary)

1-12	SLCTE1	2A6	Initial energy option SPECIFY or FISSION on card according to format.
16-27 (left adjusted)	SLCTA1 SLCTA2	2A6	Angle of incidence option SPECIFY or ISOTROPIC on card according to format.
31-48 (left adjusted)	OPT1		Output option--TRANSMISSION for transmission distribution.
	OPT2	3A6	BREMSSTRAHLUNG for radiation energy loss distribution.
	OPT3		BREMTRANS for both outputs.
49-50 (right adjusted)	IOP	12	Option for selecting increment thickness. IOP = 1 for $\Delta T$ = constant IOP = 2 for $\Delta T$ = constant/energy
51-60 (right adjusted)	NOHIST	110	Number of histories for the first output.
61-70 (right adjusted)	NCONT	110	Total number of histories for the problem.

Card 3. Initial Energy (needed only if initial energy is specified, i.e., if SLCTE1, SLCTE2 is SPECIFY)

<u>Column</u>	<u>Variable</u>	<u>Format</u>	<u>Definition</u>
1-10	EINT	E10.0	Initial energy of electrons (Mev)

Card 4. Angle of Incidence (needed only if angle of incidence is specified, i.e., if SLCTA1, SLCTA2 is SPECIFY)

1-10	THINT	E10.0	Angle of incidence in degrees.
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Card 5. Number of Slabs in Shield (Always Needed)

1-10 (right adjusted)	NOSLAB	110	Number of slabs in the shield. (Maximum of 12)
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Card 6. <sup>1</sup> Slab Description (Always Needed)

1-12 (left adjusted)	TPMT1(J) TPMT2(J)	2A6	Any 12 characters to denote material of slab J.
13-22	TMAX(J)	E10.0	Thickness of slab J ( $\text{gm}/\text{cm}^2$ )
23-32	REGNO(J)	E10.0	Number of subregions in slab J for tallying radiation losses if OPT1, OPT2, OPT3 is BREMSSTRAHLUNG or BREMTRANS, otherwise leave blank. (Maximum of 15)
33-42	A(J)	E10.0	Atomic weight of material of slab J.
43-52	Z(J)	E10.0	Atomic number of material of slab J.
53-62	ECUT(J) (J = 1, NOSLAB)	E10.0	Cut-off energy for electrons in slab J (Mev).

<sup>1</sup> One card for each slab. These should be placed in order of J = 1, 2, 3, etc.

**Card 7. Boundaries for multiple case (necessary only if transmission output is desired, i.e., if OPT1, OPT2, OPT3 is TRANSMISSION)**

<u>Column</u>	<u>Variable</u>	<u>Format</u>	<u>Definition</u>
1-10	NI	I10	Number of boundaries in entire shield for which transmission information is desired. ( $NI \geq 1$ , with maximum of 20)

**Card 8. Boundaries for Card 7.**

1-10	ZB(I)	7E10.0	Z coordinate of boundaries for which transmission information is desired ( $gm/cm^2$ )
11-20			in order of increasing magnitude.
etc.	(I = 1, NI)		(If $NI = 1$ , ZB(1) = thickness of shield.)

**Card 9.**

1-10	FACTOR	E10.0	Constant used to determine increment thickness, $\Delta T$ .
11-22 (right adjusted)	RAND1	J12	Number to start random number generator. Should consist of at least 8 digits with the right most digit being <u>odd</u> .

**Card 10.<sup>2</sup>**

1-10	IMAX(J)	I10.	Number of energies for range-ionization energy loss tables for material of slab J. (Maximum of 50)
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**Card 11.<sup>2</sup>**

1-10	ENERGY(I, J)	7E10.0	Energy in order of increasing magnitude (Mev).
11-20	RANGE(I, J)		Range of electron of above energy ( $gm/cm^2$ )
21-30	RATE(I, J)		Rate is $dE/dx$ or ionization energy loss of electron of above energy ( $Mev\ cm^2/gm$ )
31-40			
etc.	(I = 1, IMAX(J))		

<sup>2</sup> Set of cards 10 and 11 for each slab J. These should be in order of  $J = 1, 2, \dots$

**Card 12. (Always Needed)**

<u>Column</u>	<u>Variable</u>	<u>Format</u>	<u>Definition</u>
1-10 (right adjusted)	L1	I10	Number of energy bins for tallying transmission distribution and radiation energy losses. (Maximum of 20)

**Card 13. (Always Needed)**

1-10	ENGY(I)	7E10.0	Energy bins for tallying transmission and radiation energy losses (Mev) in order of increasing magnitude. The number will be the maximum energy for bin I.
11-20			
etc.	(I = 1, L1)		

**Card 14. (Always Needed)**

1-10	L2	I10	Number of angle bins. (Maximum of 30)
------	----	-----	---------------------------------------

**Card 15. (Always Needed)**

1-10	ANGLE(I)	7E10.0	Angle bins for transmission tally (degrees) in order of increasing magnitude. The number will be the maximum angle for bin I.
11-20			
etc.	(I = 1, L2)		

**Card 16. (Necessary only if NCONT > NOHIST)**

1-10	NOHIST	I10	Number of histories for next output.
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There can be as many of card 16 as desired. An output edit is performed after completion of number of histories indicated by NOHIST. The only criteria is that the sum of the NOHIST for any problem must equal the number output for NCONT.

More than one problem can be run at a time. With the exception of the permanent data tables, the above input (cards 1 through 16) will be repeated for each problem and will be placed in succession in the data deck.

This data is input on punched IBM data cards.

TABLE 3. Set 1. Values of  $\nu$ , and Integrals of Functions Integrated from 0 to  $\nu$ ,

<u>Column</u>	<u>Variable</u>	<u>Format</u>	<u>Definition</u>
1-6	UPLIM(I)	E6.0	$\nu$
7-16	FZINT(I)		$\int_0^\nu f^{(0)} \nu^i d\nu^i$
17-26	F1INT(I)	3E10.0	$\int_0^\nu f^{(1)} \nu^i d\nu^i$
27-36	F2INT(I)		$\int_0^\nu f^{(2)} \nu^i d\nu^i$
37-42	UPLIM(I)	E6.0	$\nu$
43-52	FZINT(I)		$\int_0^\nu f^{(0)} \nu^i d\nu^i$
53-62	F1INT(I)	3E10.0	$\int_0^\nu f^{(1)} \nu^i d\nu^i$
63-70	F2INT(I)	I = 1, 128	$\int_0^\nu f^{(2)} \nu^i d\nu^i$

TABLE 4. Set 2. Tables of X and Exponential Integral  $E_1(X)$

<u>Column</u>	<u>Variable</u>	<u>Format</u>	<u>Definition</u>
1-10	$ARG(I)$		X
11-20	$E1(I)$		$E_1(X)$
21-30	$ARG(I)$	6E10.0	X
31-40	$E1(I)$		$E_1(X)$
41-50	$ARG(I)$		X
51-60	$E1(I)$		$E_1(X)$
		I = 1, 128	

## OUTPUT DATA

The output consists of a summary of the input including the number of histories, source energy, angle of incidence, method used to select increment thickness,  $\Delta T$ , number of slabs in the shield and their respective thicknesses, the number of transmission boundaries and these boundaries. These items are identified in the output. If the input specified that the transmission array is desired, this is then printed. The number of electrons transmitted in each energy and angle bin is under the heading N and the sum of the energy of the electrons transmitted in each energy and angle bin is under the heading E. The angle and energy bins are considered to be  $0 - E_1$ ,  $E_1 - E_2$ , etc., and  $0 - A_1$ ,  $A_1 - A_2$ , etc. The number and energy transmitted for each angle is summed over all energies. Then the total number transmitted is recorded. In the case where there is more than one transmission boundary, the number backscattered (transmitted at angles from  $90-180^\circ$ ) is valid only for the case of the thickest slab.

If the radiation energy loss throughout the shield is desired, this array follows the transmission distribution. This array gives the number of times the radiation energy was between energies  $0 - E_1$ ,  $E_1 - E_2$ , etc., for regions of a slab. This array is written for each slab,  $J = 1$  to the total number of slabs of the shield. Each of the regions of the slab has a thickness equal to the thickness of the slab divided by the total number of regions in the slab.

## OPERATING INFORMATION

### MACHINE SET-UP AND RUN INFORMATION

#### General Machine Operation

Machine set-up would be as for any program under the FORMON system using no tapes other than A2 (logical 5) for input and A3 (logical 6) for output, and no special switch settings.

Normal exit from the program occurs when the output from the last problem is completed and there is no more input to be read in. Error stops occur when there is either an error in spelling on the input option card or there is an error in calculation. In the case of the former, the appropriate comment is written. For the latter, a value for the error indicator, KERROR, is written. The error indicators and their corresponding errors are as follows:

KERROR = 2

Error in subroutine MOLLI. Value of b < 1.

Check input values of atomic weights and atomic numbers, and the factor for computing the path increment  $\Delta T$ .

= 3

Error in subroutine RANDE. Check input tables of range, average ionization loss and the corresponding energies. This error occurred because the table was exhausted without finding a value.

= 4

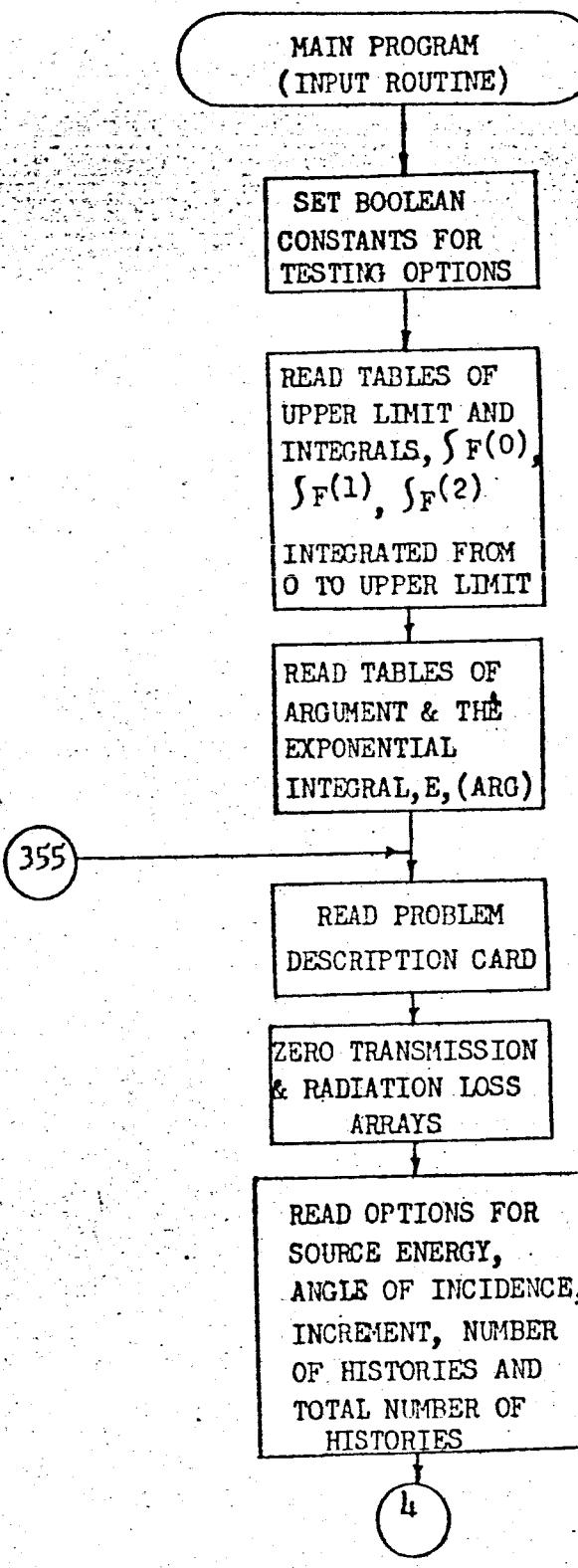
Error in subroutine TLYRD. The radiation energy loss was greater than the values of the energy bins.

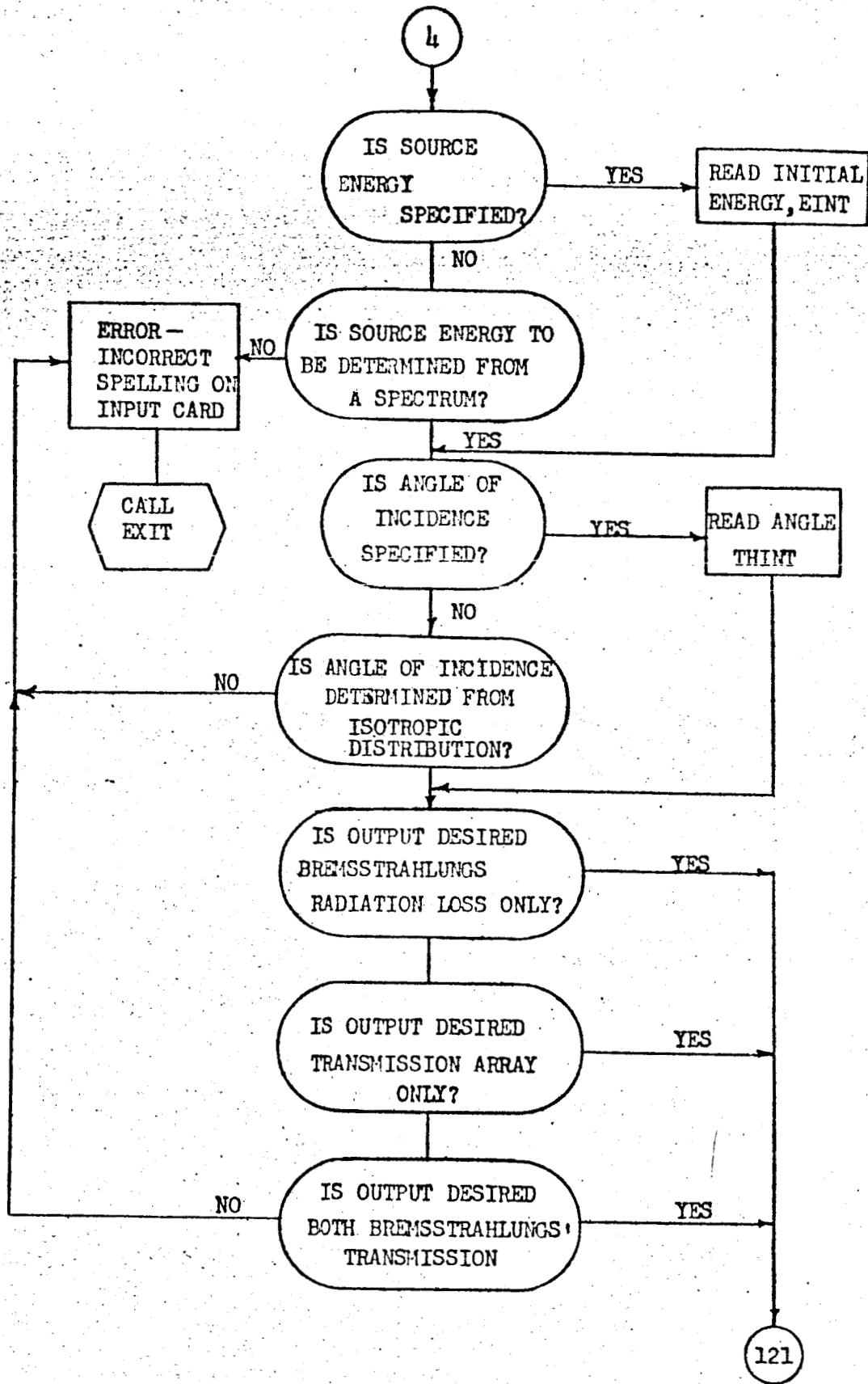
KERROR = 4 (cont'd)      Check to see that the last energy bin is as large  
as or greater than the initial energy of the  
electron.

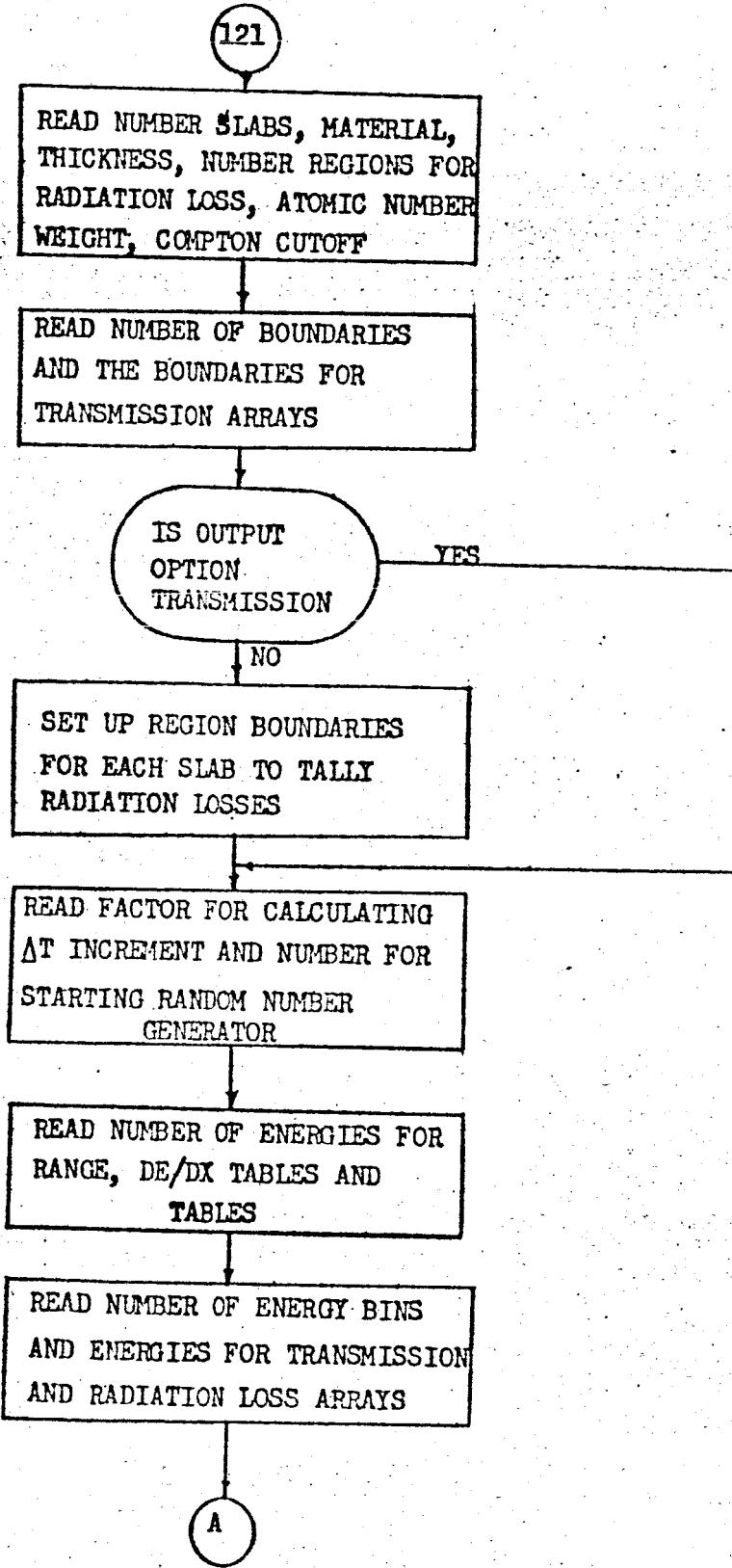
## **PROGRAMMING INFORMATION**

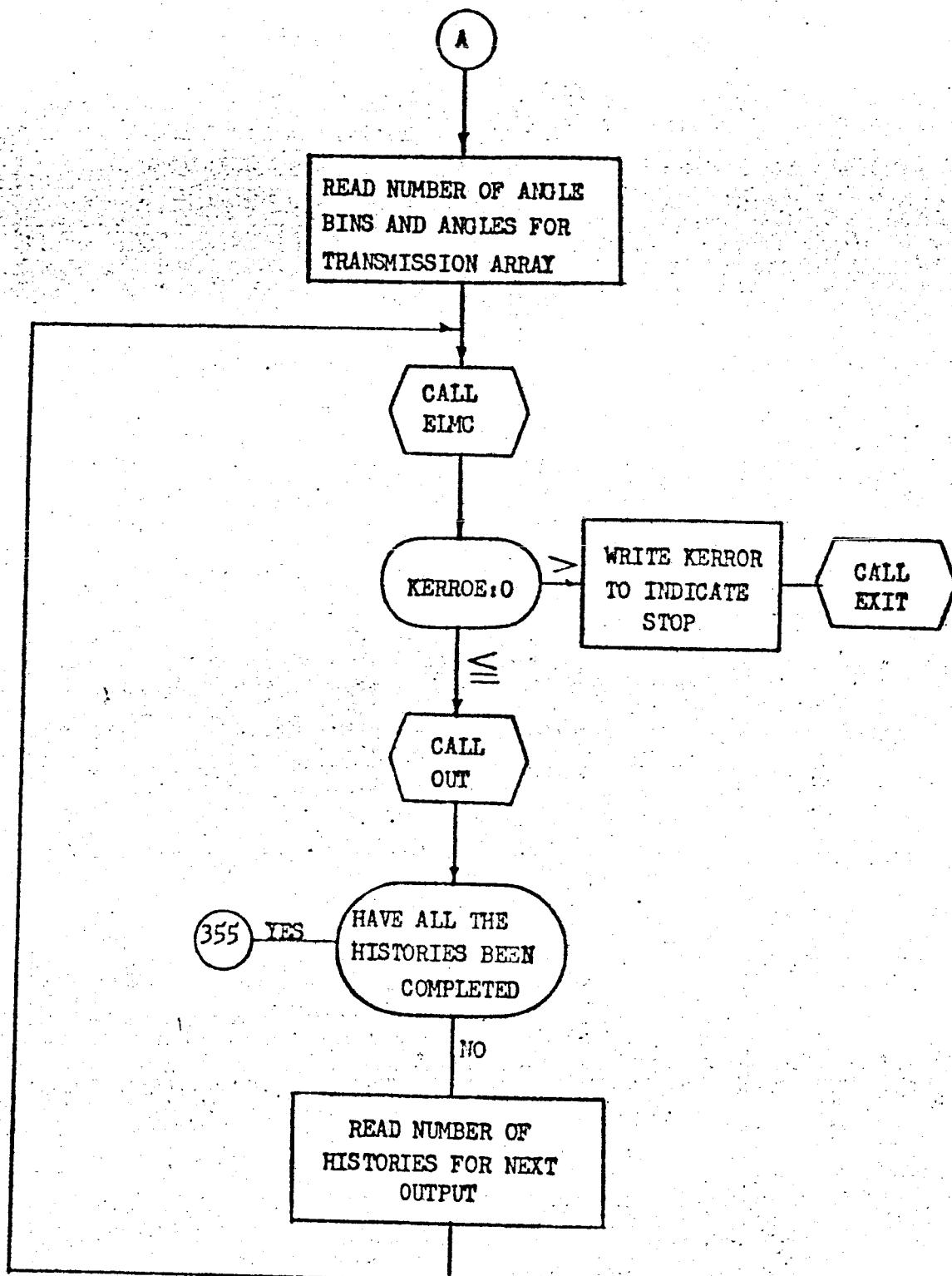
This portion of the report contains the programming information and consists of Flow Charts,  
**Program Listing, Sample Input Data and Sample Problem.**

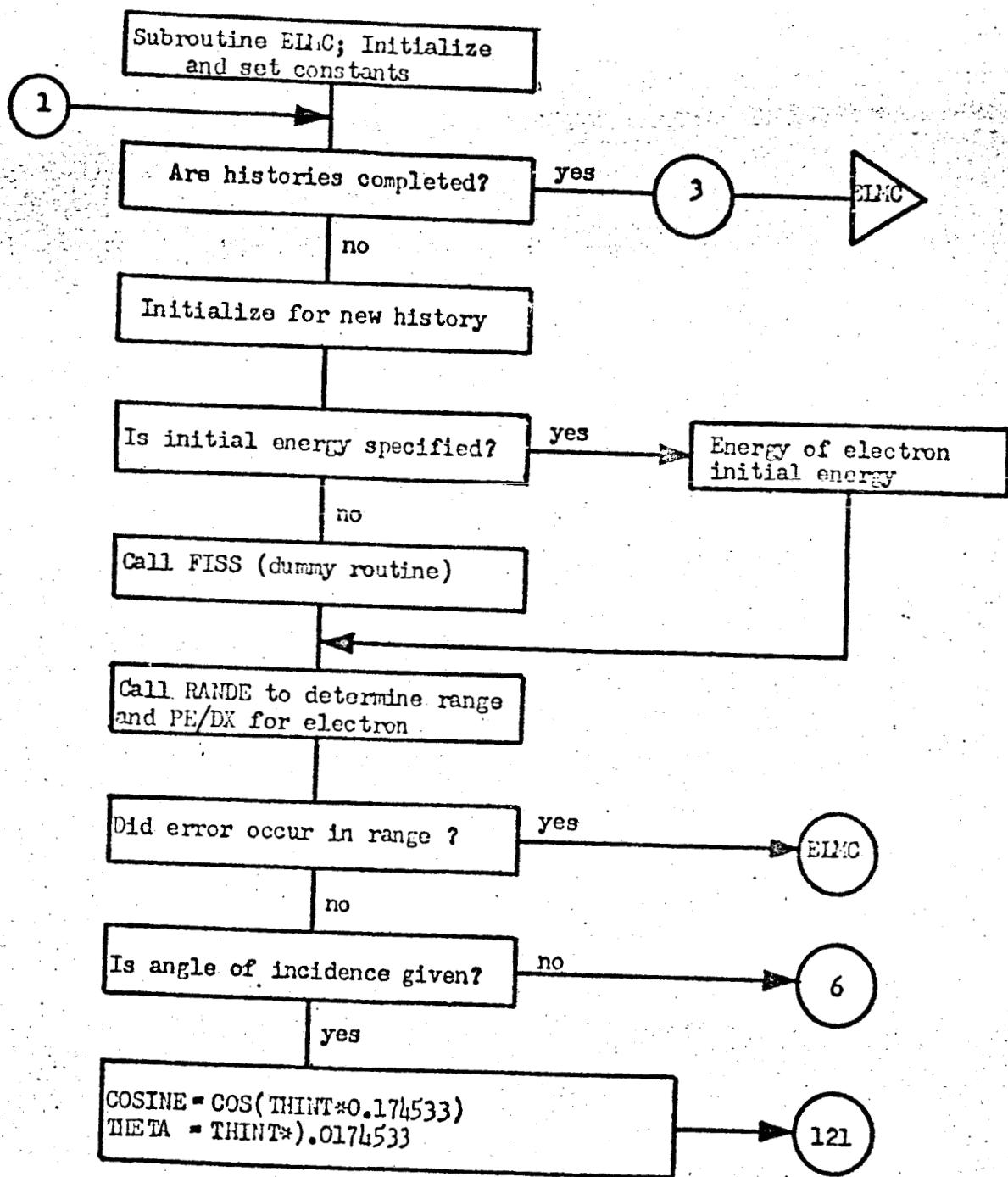
## **FLOW CHARTS**





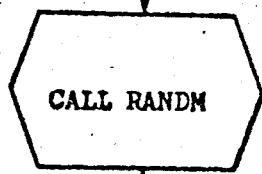






Subroutine ELMC

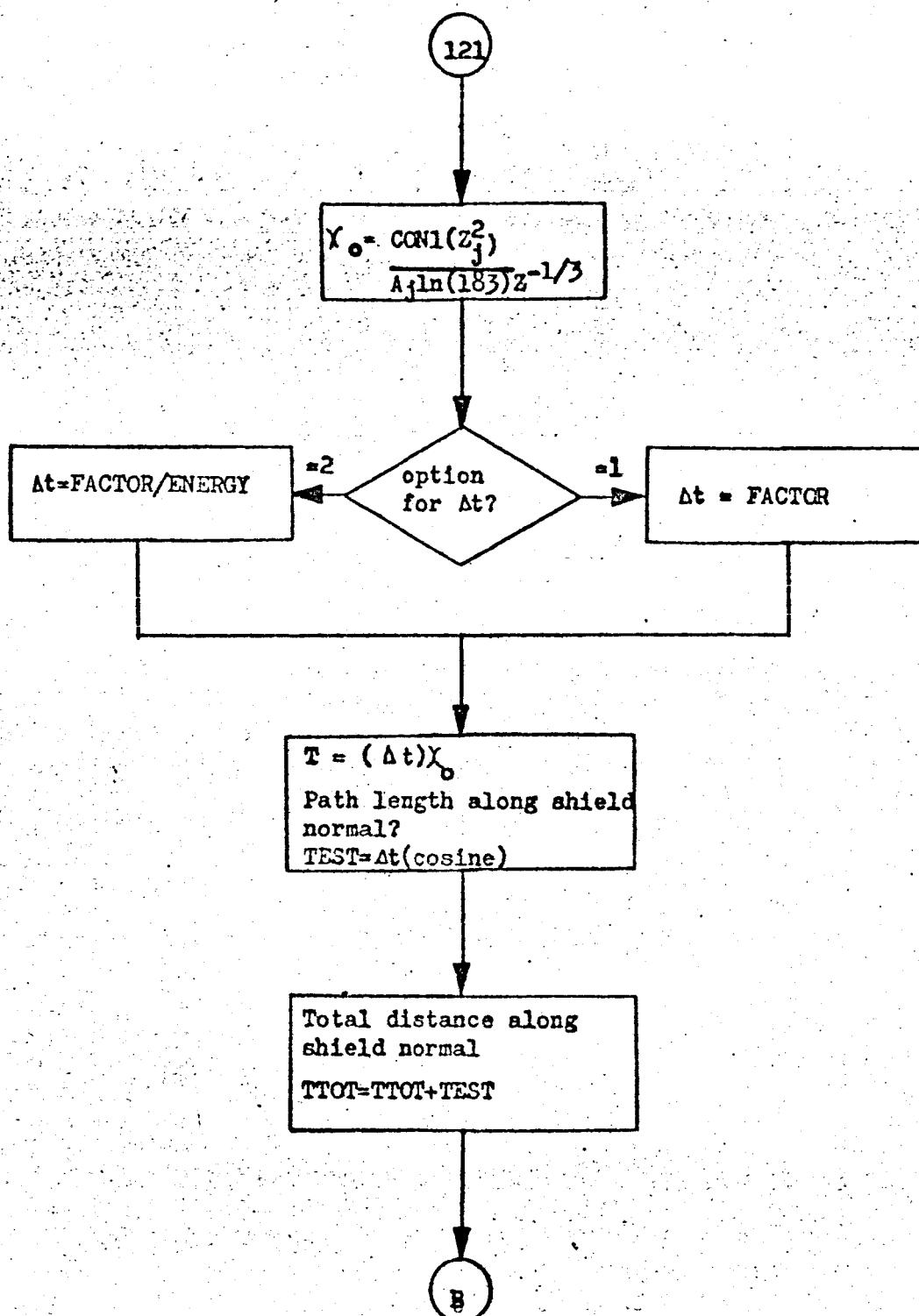
6

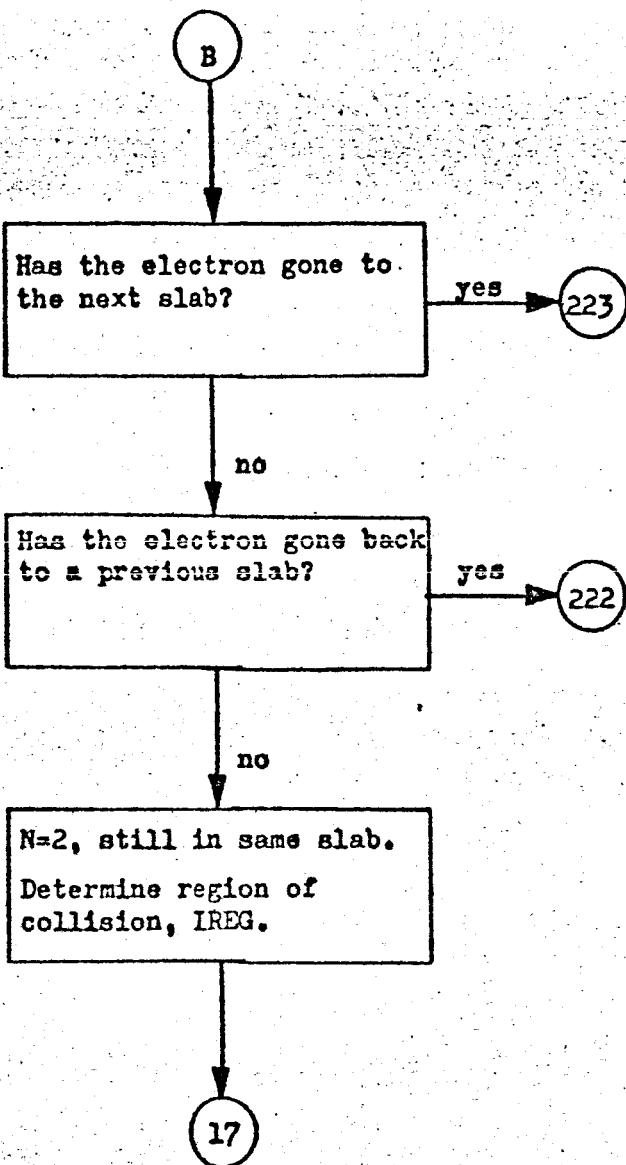


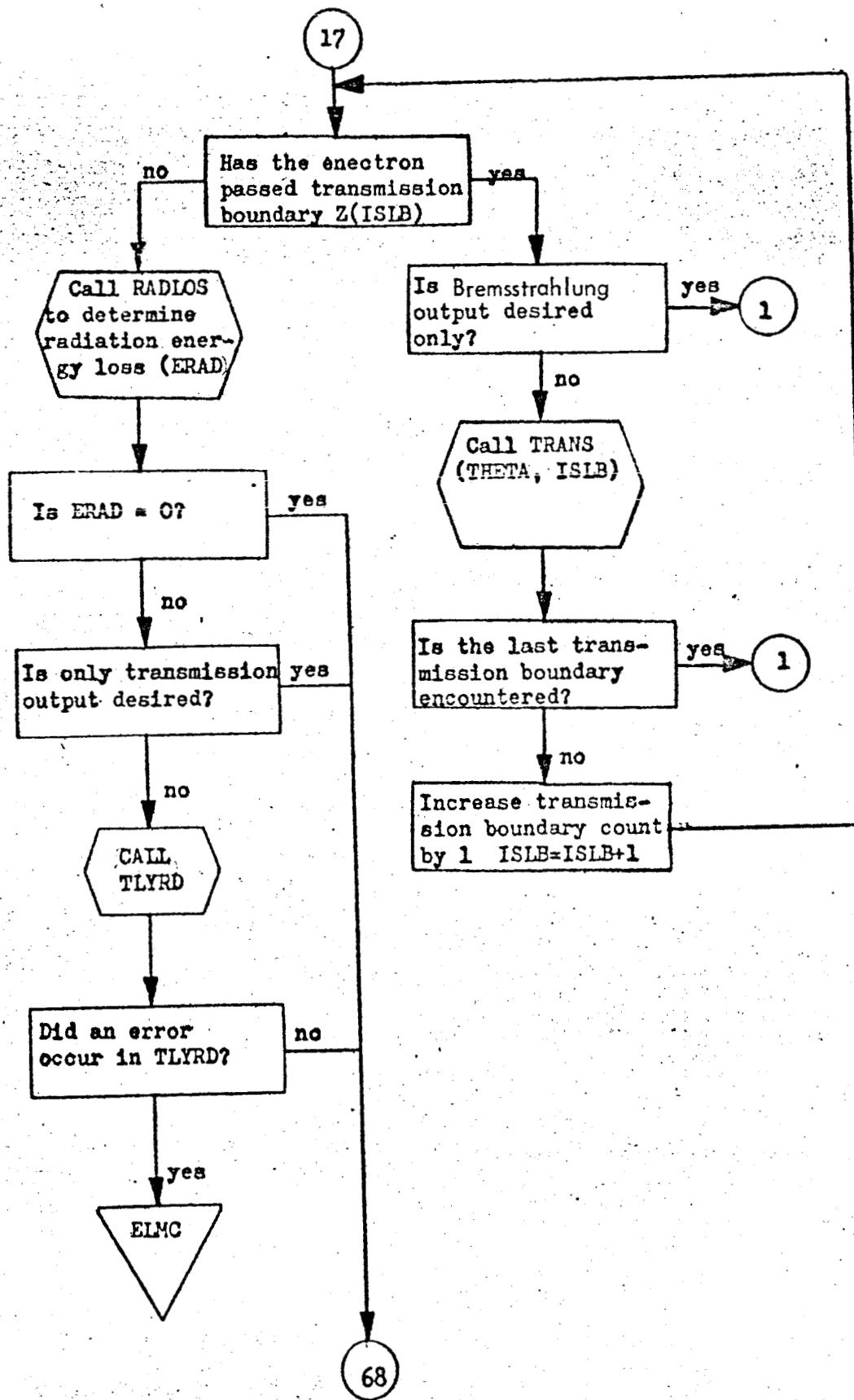
Cosine = random  
number

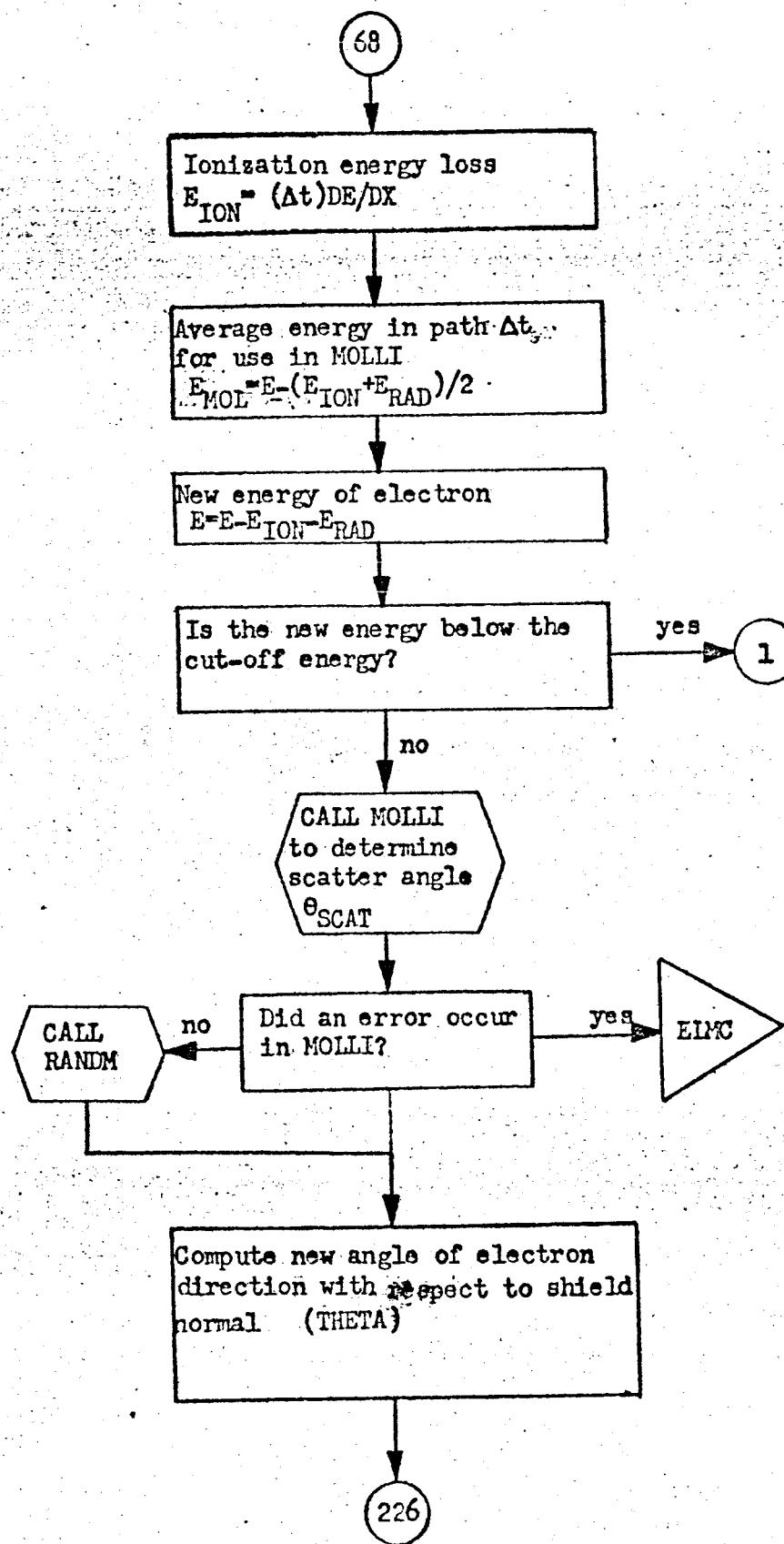
THETA =  
 $\text{Cos}^{-1}(\text{cosine})$

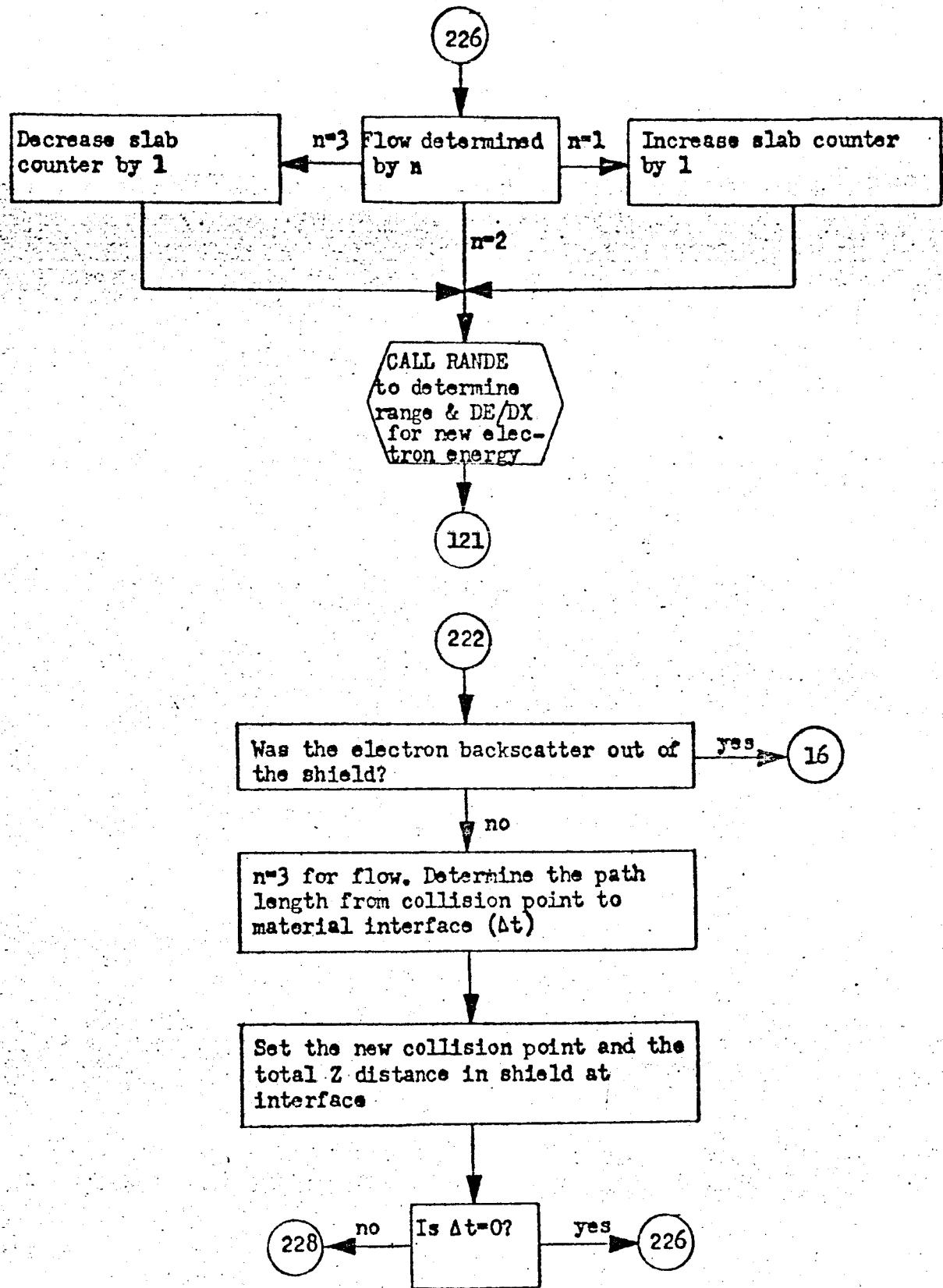
121

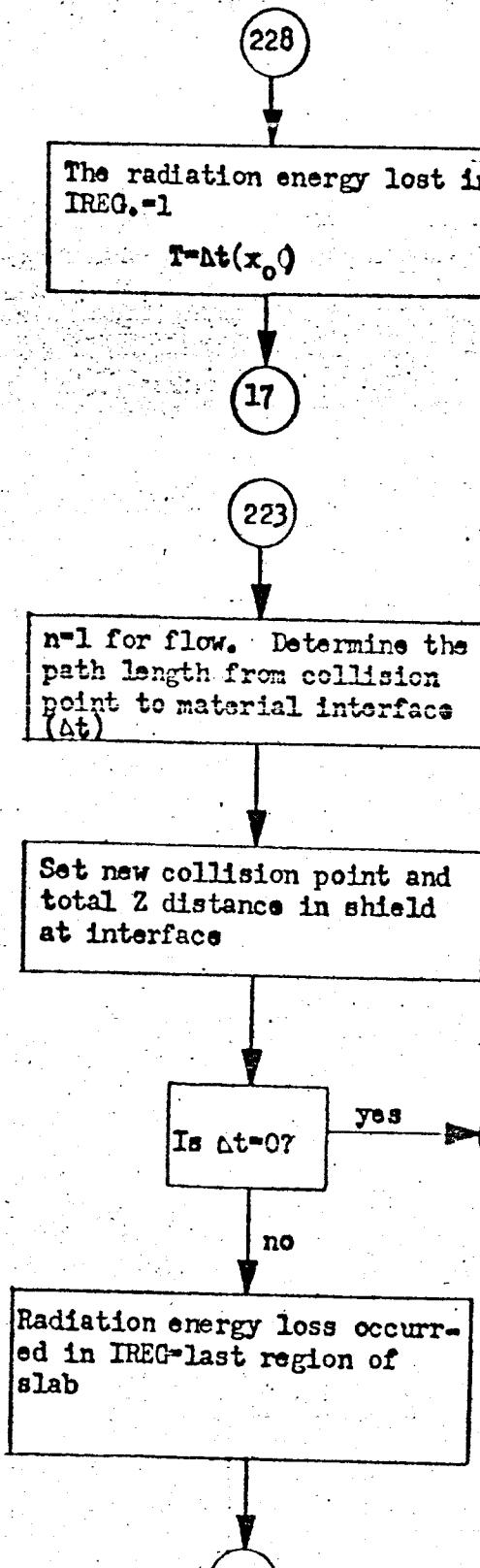


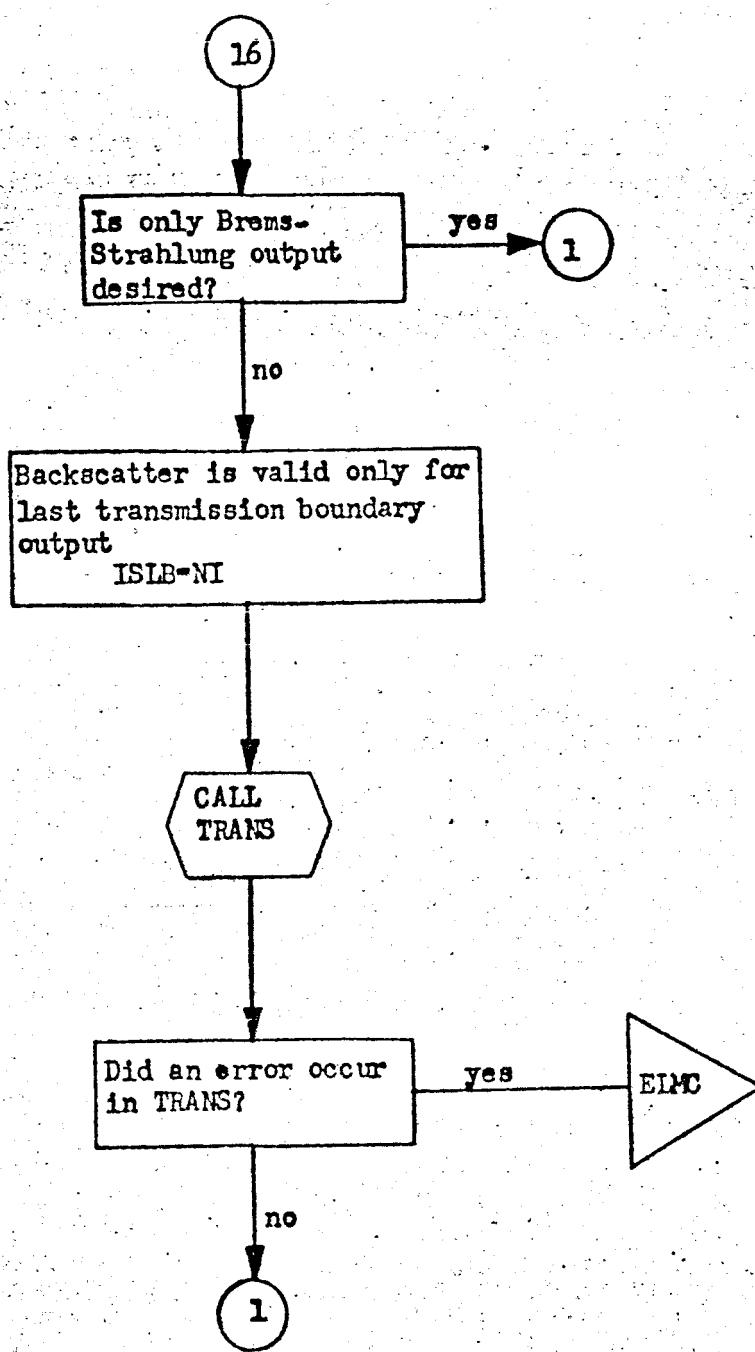




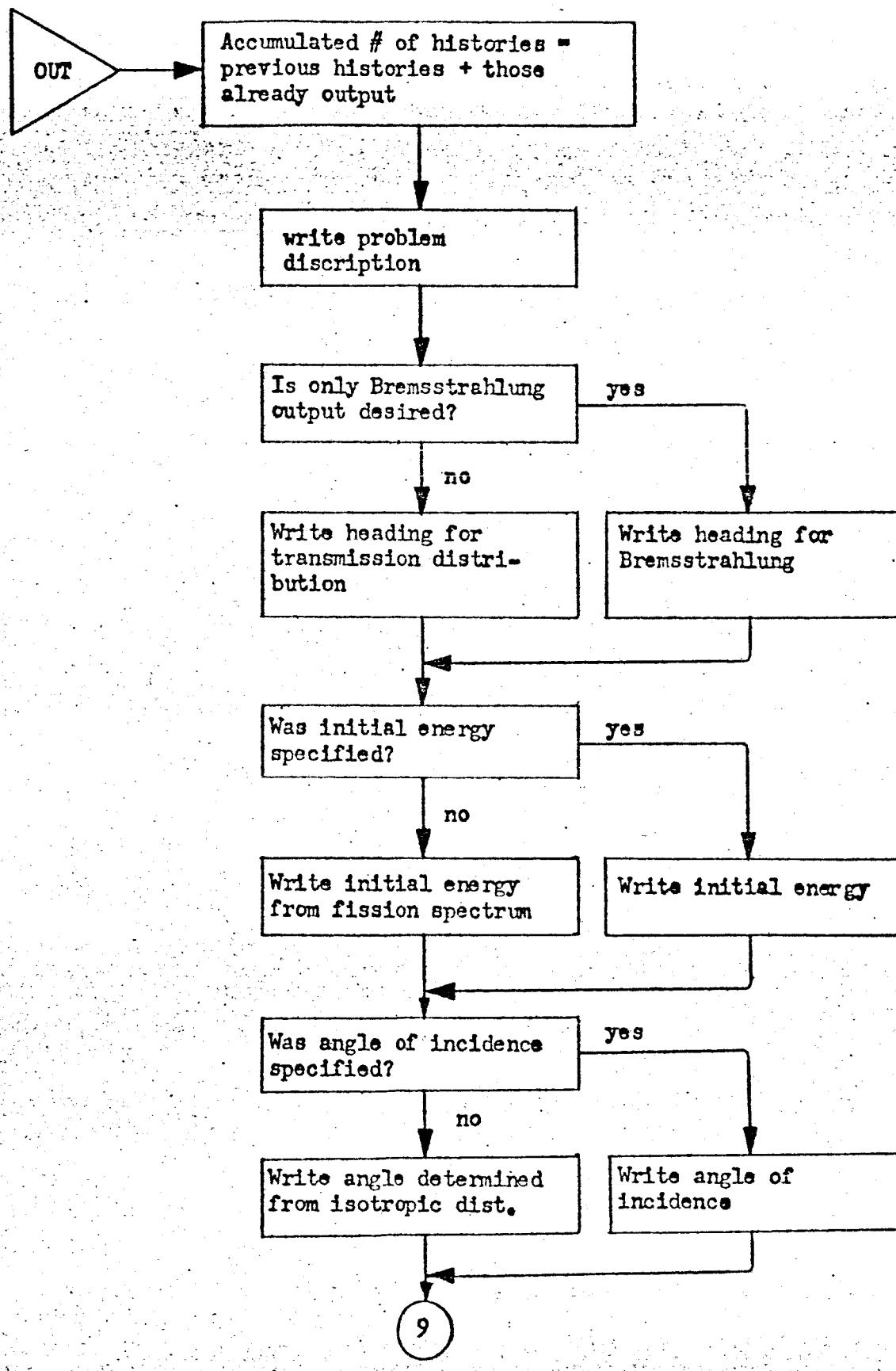


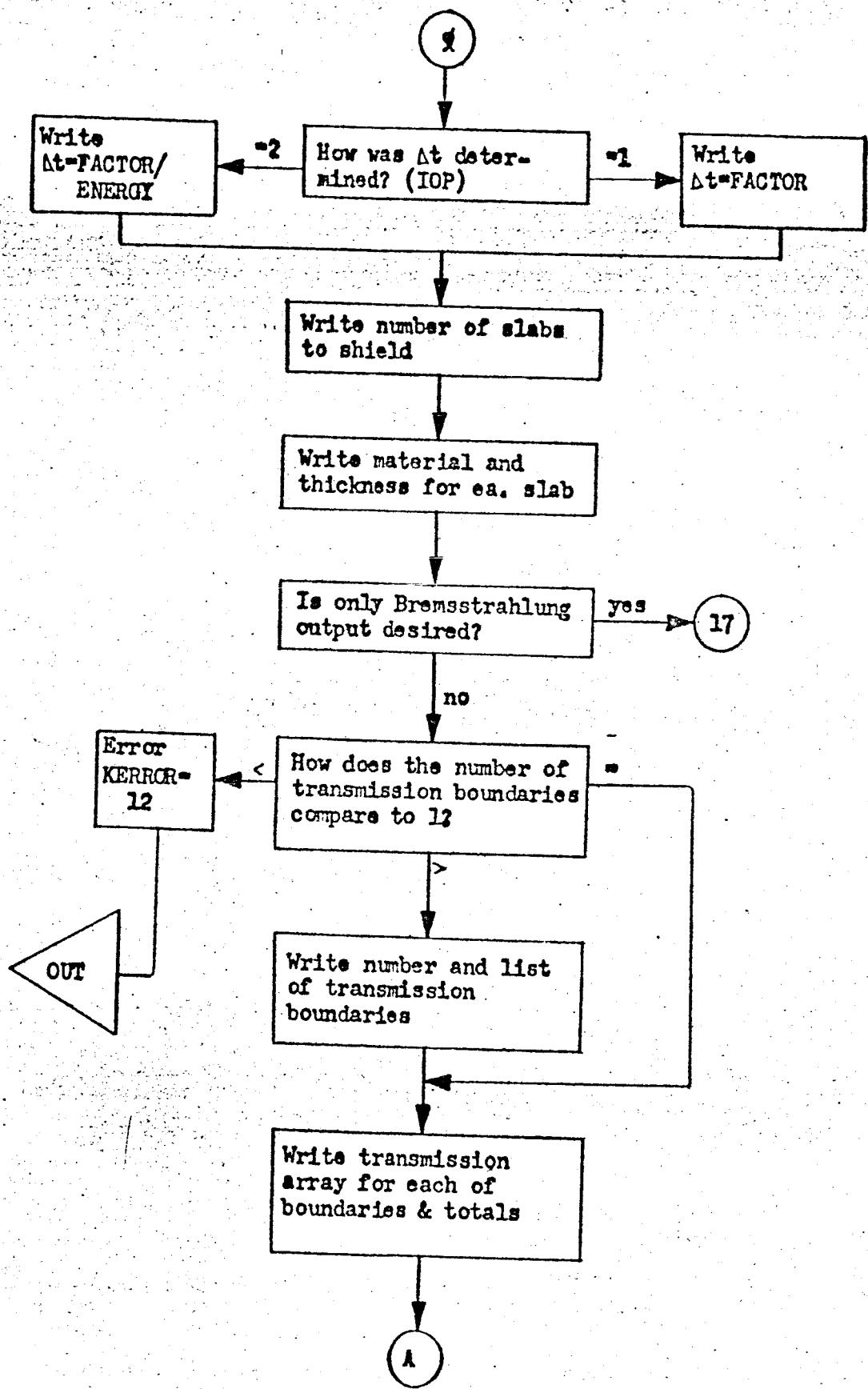


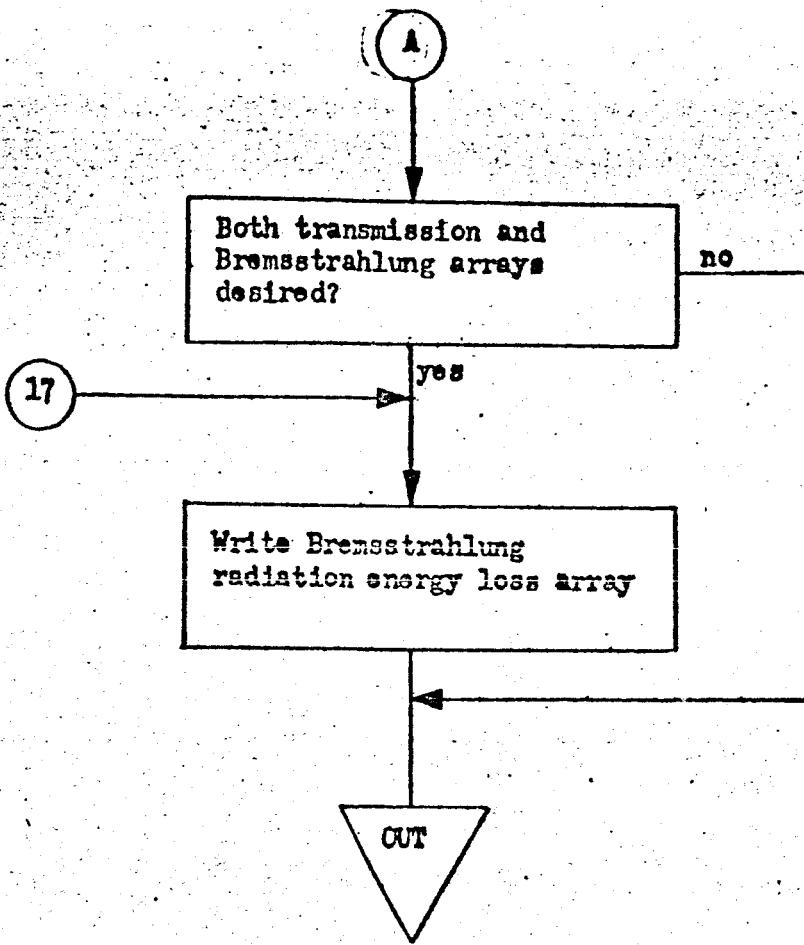


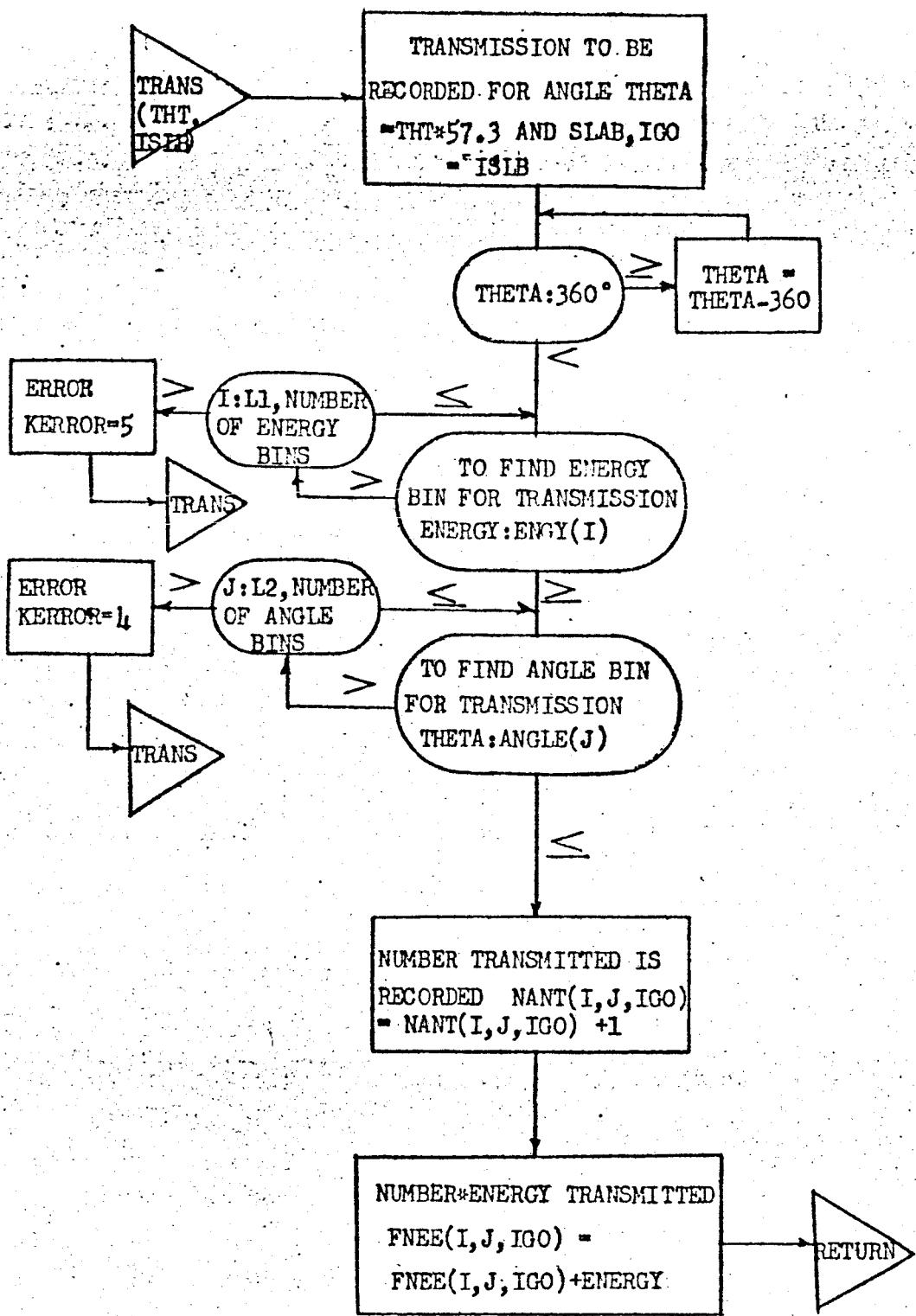


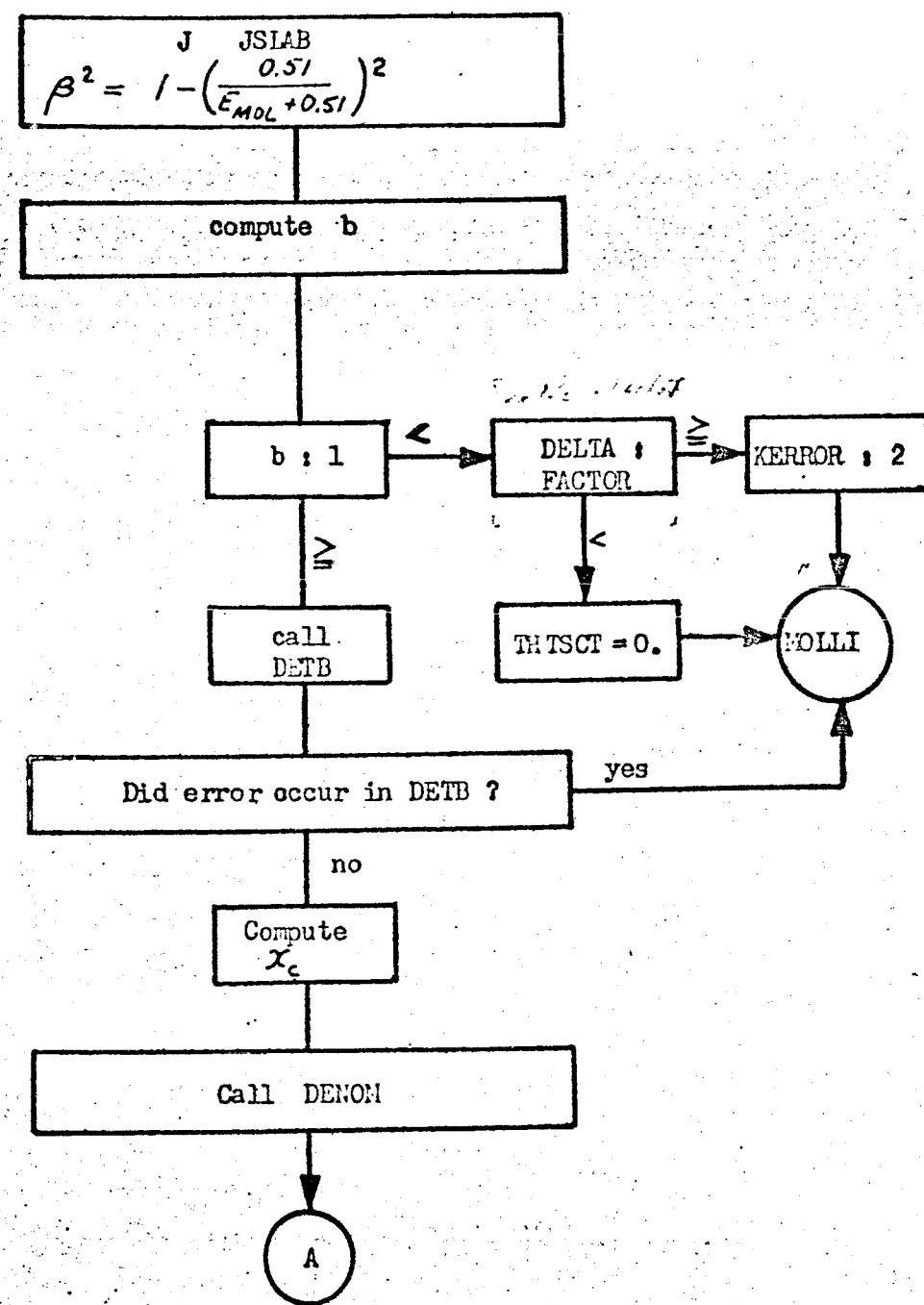
Subroutine OUT



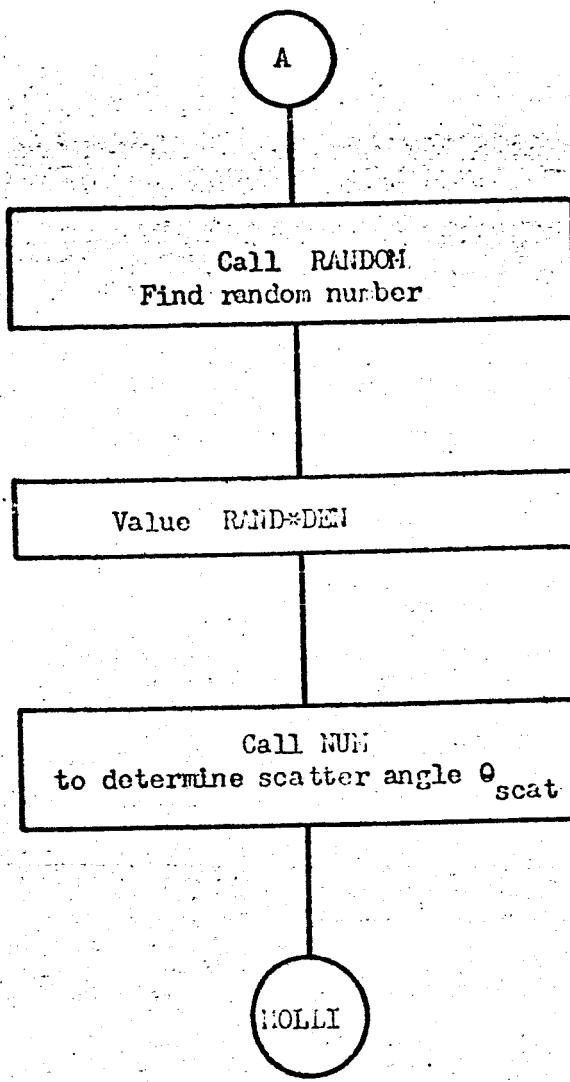






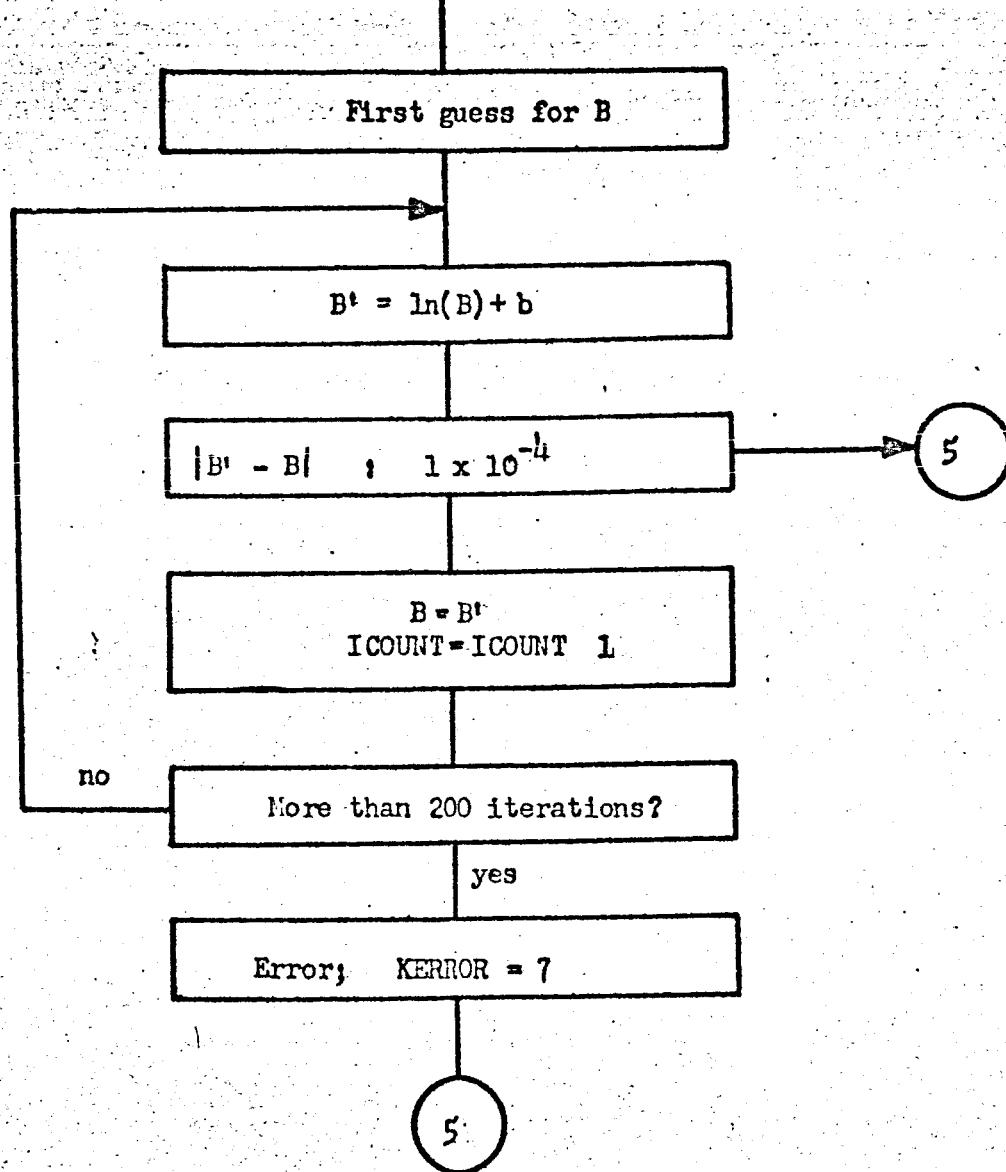


Subroutine MOLLI  
(page 1 of 2 )

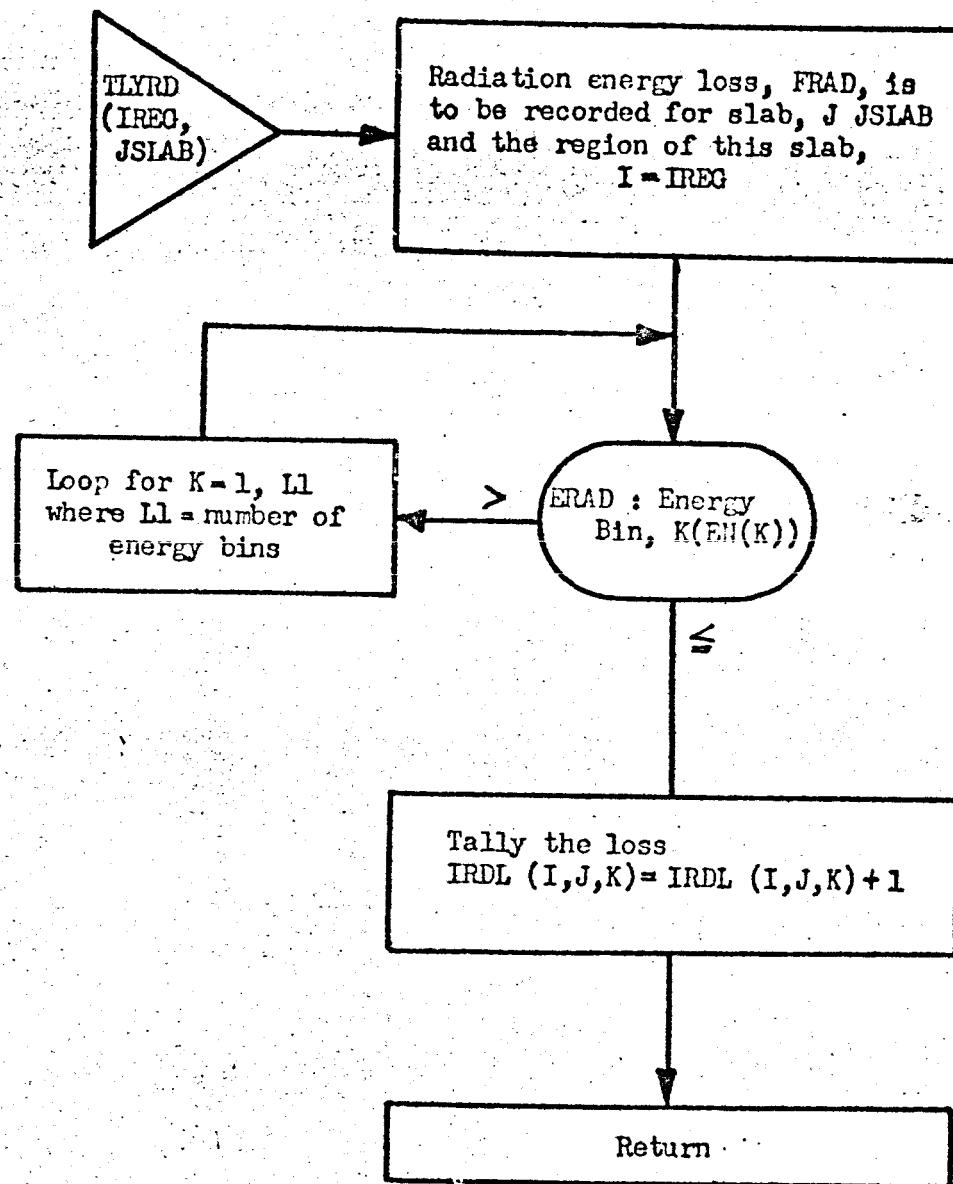


Subroutine MOLLI  
(page 2 of 2 )

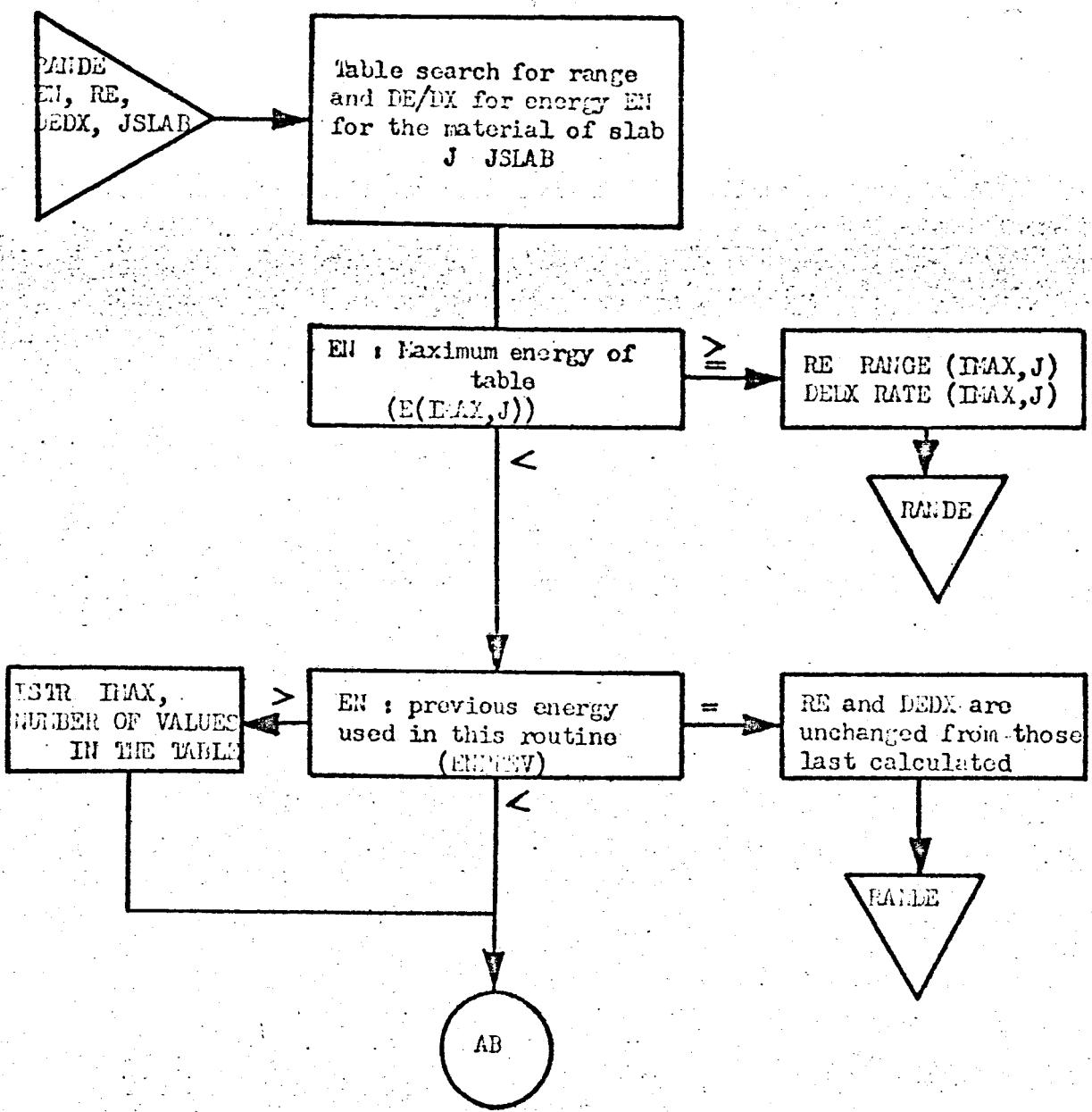
Slope of a plot of B's versus  
b's is 0.9075804  
Iteration counter ICOUNT = 0



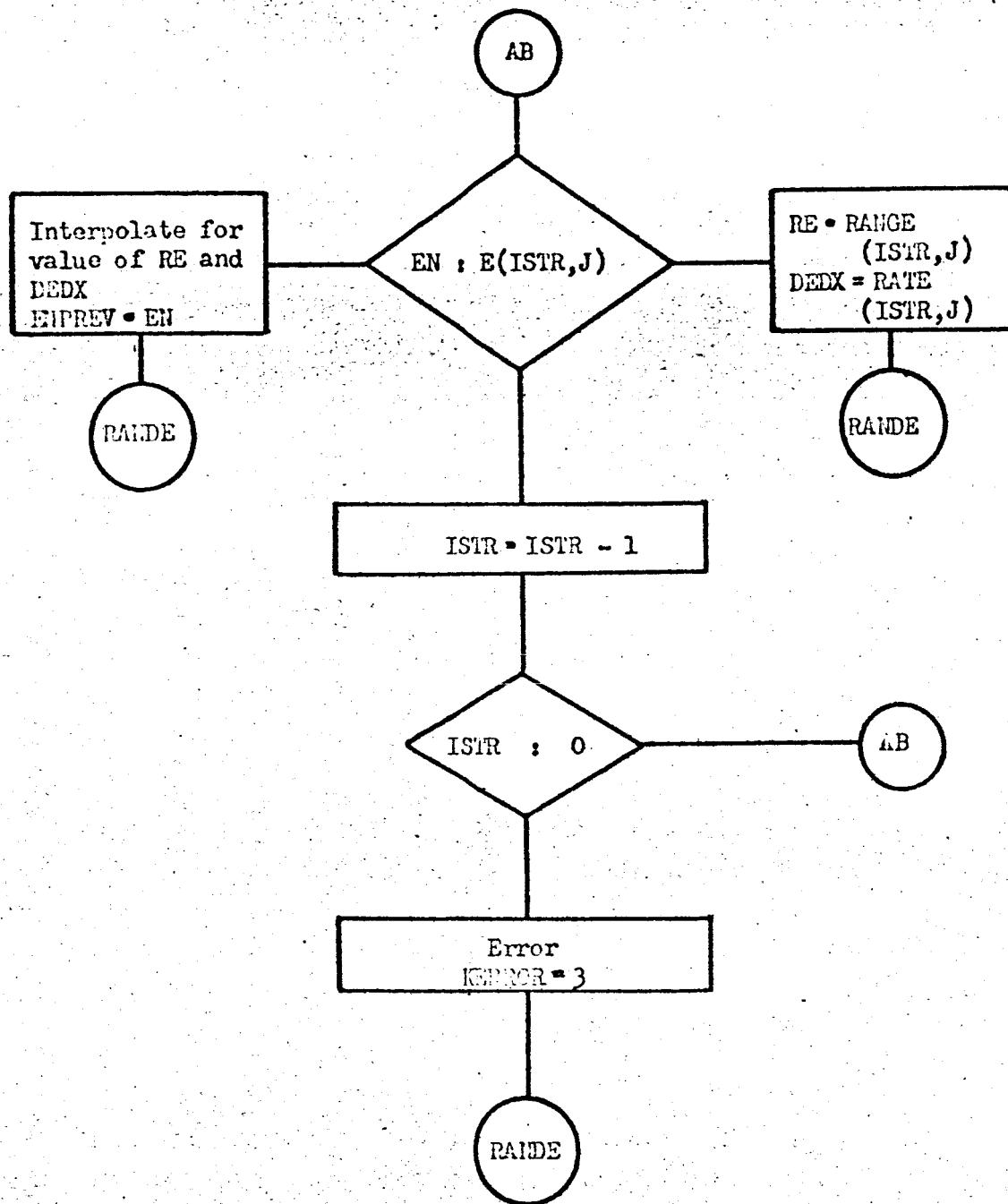
Subroutine DETB



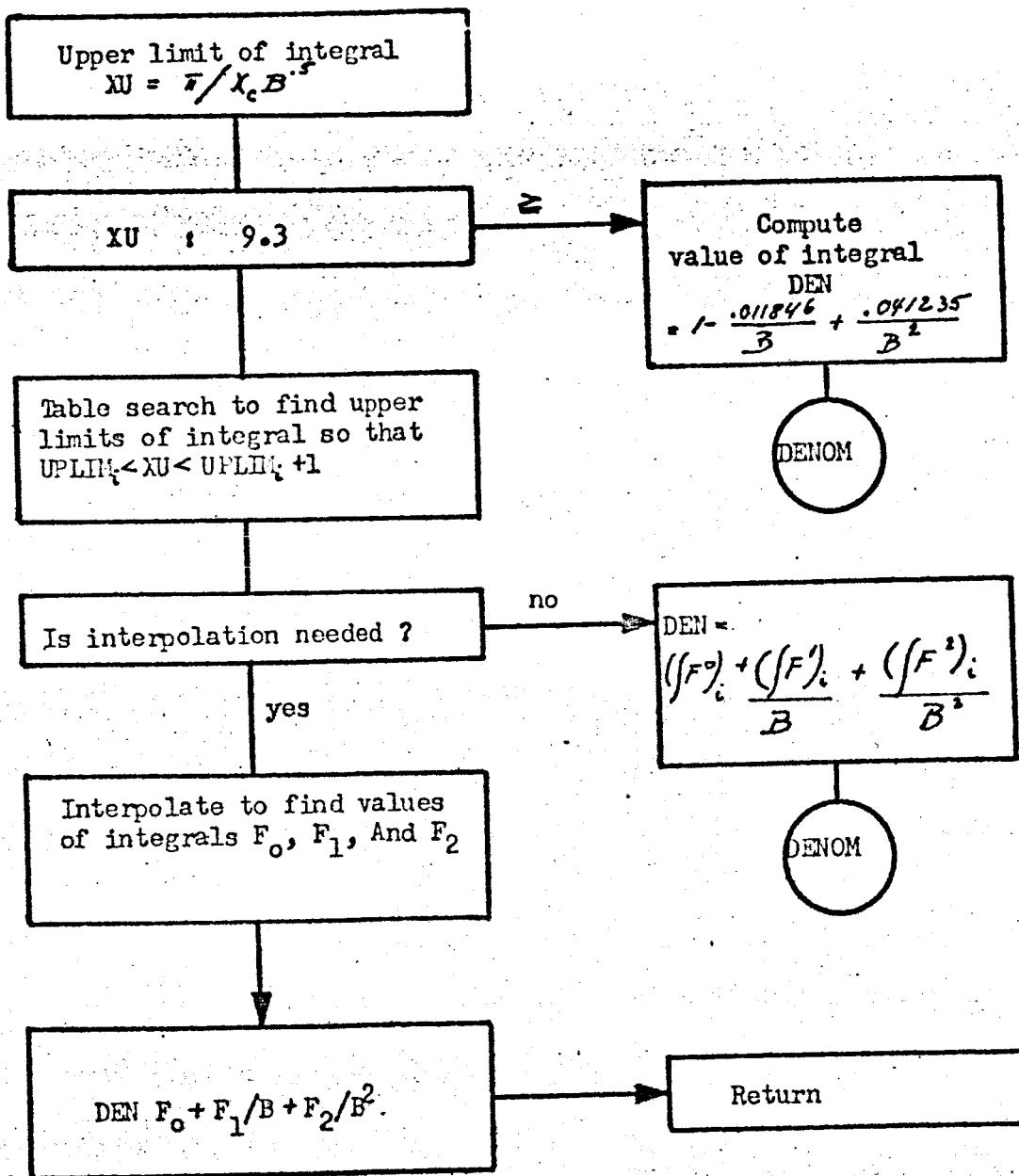
Subroutine TLYRD



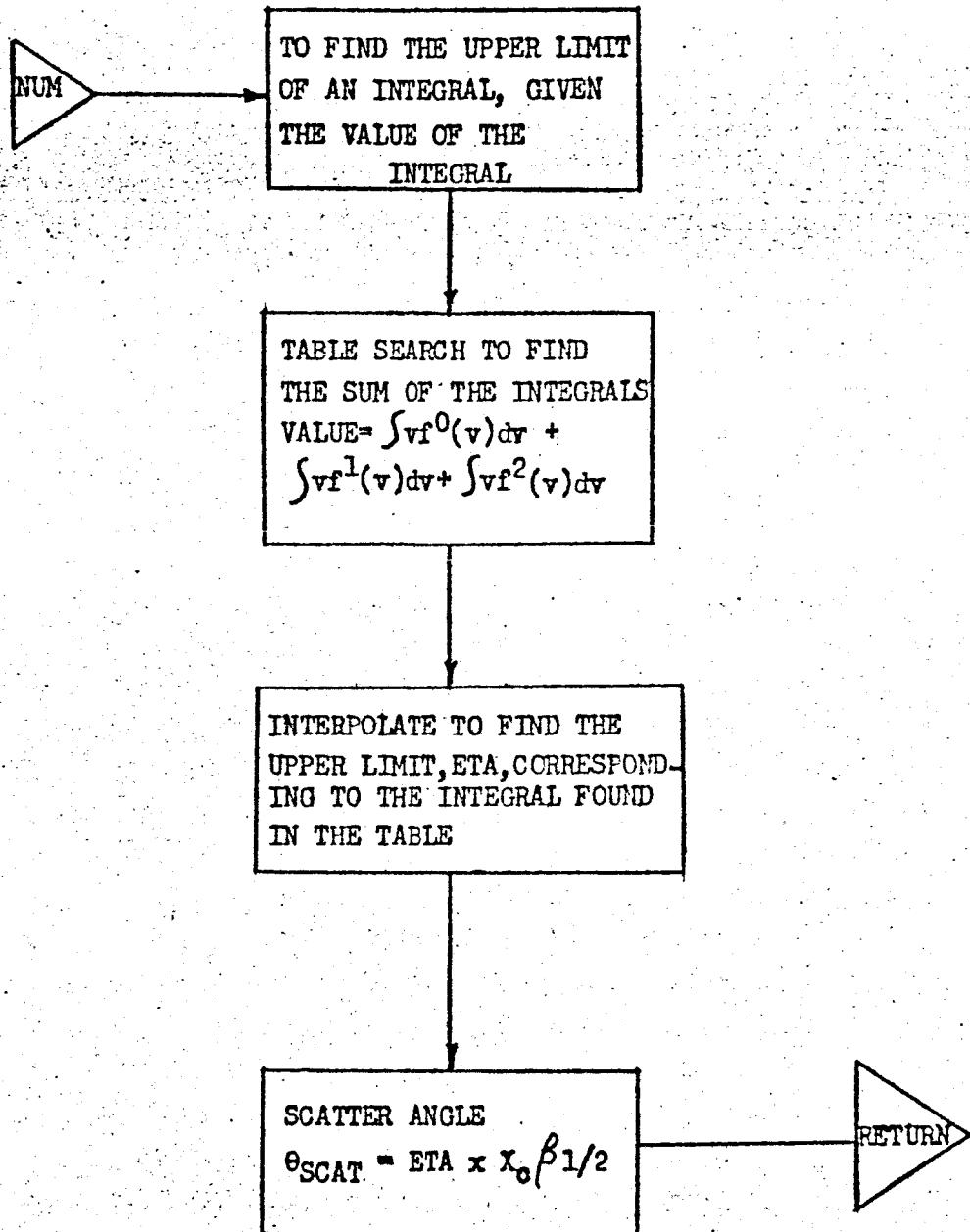
Subroutine RANDE  
Page 1 of 2

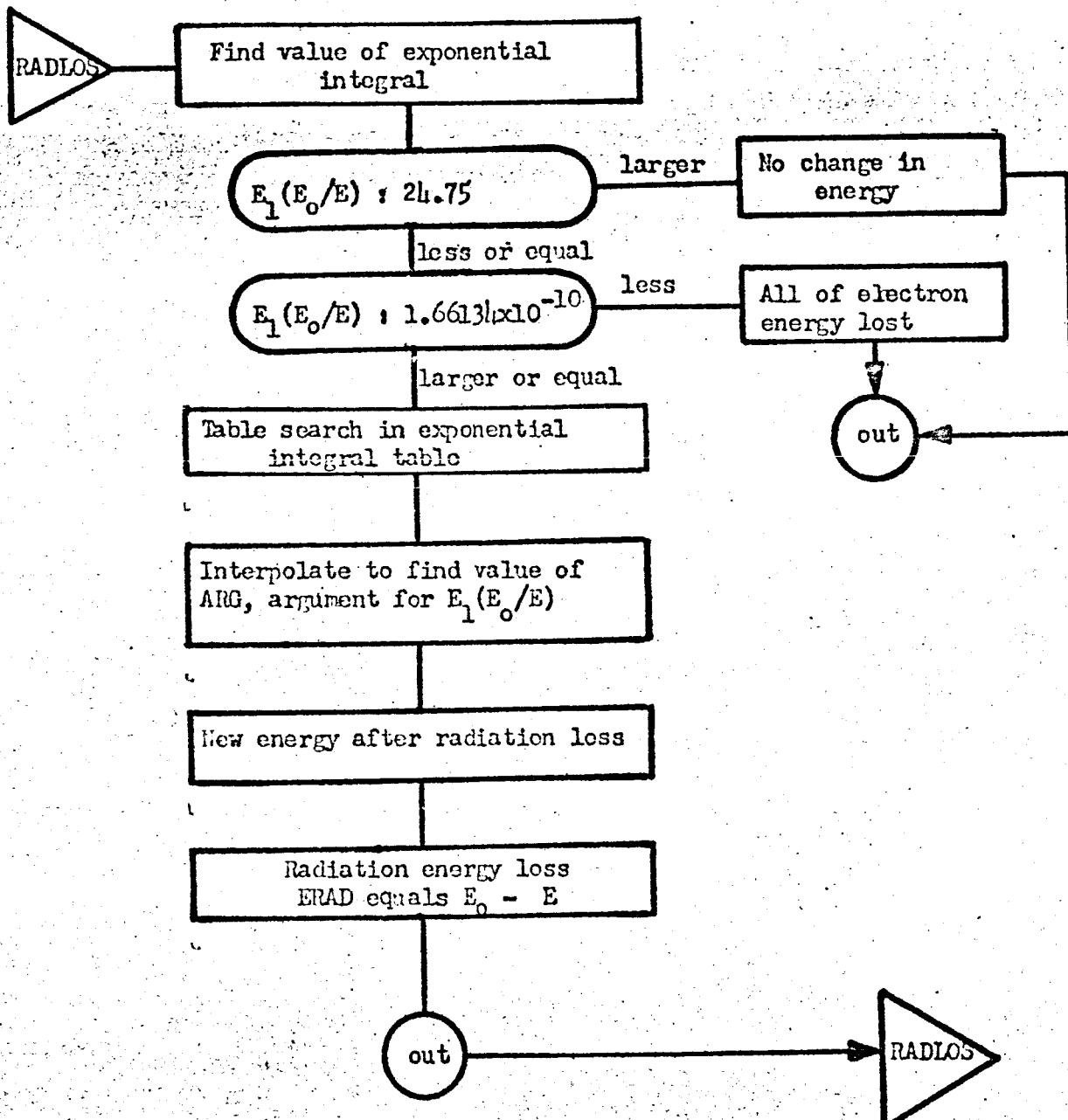


Subroutine RAIDE  
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Subroutine DENOM





Subroutine RADLOS

## **PROGRAM LISTING**

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```

COMMON/HMAX,KANGE,RATE,ENERGY,DUM1,E1,DUM2,ARG,DUM3,UPLIN,
10 DUM4,FZINT,DUM5,FLIN1,DUM6,F214T,DISCPT,ECUT,TMAX,Z,A,REC,TPM11,
21 TPM12,REGNO,ENSY,ANGLE,YOSLAB,UNHIST,SLCT1,SPCFY,EINT,SLCT1A,SPACE
31 THINT,OPT1,BREM,FACTOR,TRA,ROUH,L1,L2,BLANK,KERROR,NANT,IRDL,SPACE
4, RAN01,RAND,CDF12,ZR,IOP,N1,F1,E1,ISUM
DIMENSION 1 MAX(12),RAN01(50,12),KATE(50,12),ENERG(50,12),E1(128),
1 ARG(128),FLIM(128),F214T(128),FLINT(128),F214T(128),DISCPT(12),
2 TMAX(12),A(12),REG15,12),TPM1(12),TPM2(12),REGD(12),ENSY
3(LIB) ANGLE(16),BLANK(7),SPACE(6),LB(20),FIEE(15,16,20),ECUT(12),
4,NANT(15,16,20),IRDL(15,12,15)
SPCFY=624725233126
B   F1SS=263162623146
B   SIPC=316246635146
B   EXITM=225125446762
B   TRA=63512456244
B   BOTH=225125446351
B   READ ALL TABLES
C   TABLES FOR INTEGRALS
C   1 READ INPUT TAPE 5,10,(UPLIM(1),FLINT(1),FLINT(1),1=1,128)
10 FORMATE(6.0,3E10,0,E6.0,3E10,0)
C   TABLES OF E1(X)
C   2 READ INPUT TAPE 5,20,(ARG(1),E1(1),1=1,128)
20 FORMAT(6E10,2)
C   END OF TABLES
C   355 READ INPUT TAPE 5,110,(DISCPT(1),1=1,12)
110 FORMAT(12A6)
1 ISUM=0
DO 356 I=1,15
DU 356 J=1,16
DC 356 K=1,20
NANT(1,J,K)=0
356 FEE(I,J,K)=0.
DO 357 I=1,15
DC 357 J=1,12
DC 357 K=1,15
357 IRDL(I,J,K)=0
C   READ OPTIONS AND NUMBER OF HISTORIES
3 READ INPUT TAPE 5,30,SLCT1,SLCT2,SLCT1A,SLCT2A
10 FPT1,OPT2,OPT3,ICP1
30 FORMAT(2A6,3X,2A6,3X,3A6,12,2110)
C   CHECK OPTION INPUT
4 IF(SLCT1-SPCFY)<6,5
C   ENERGY IS SPECIFIED IN INPUT
6 ACAC INPUT TAPE 5,40,CLNF
40 FDISCPT(1,1)=0
5 IF(SLCT1-FSS)>7,8,7
C   ENERGY IS UNKN
C   7 WRITE OUTPUT TAPE 5,50
50 FDISCPT(1,1)=STOP -- MISSPELLING ON INPUT CARD
CALL EXIT
C   8 IF(SLCT1-SPCFY)>9,1000,9

```



## SUBROUTINE ELMC

```

C ELECTRON MONTE CARLO
C COMMON SPACE,ECUT,TMAX,Z,A,REG,IPMT1,IPMT2,REGD,BLANK,
C INSLAB,NHIST,SLECTE,
C ISPCFY,EINT,SLECTA,THINT,OPTION,BREM,FACTOR,TRA,BOTH,L1,L2,
C 2ENPKEV,ERAD,THTSCT,T,CUBE,EMUL,DELT,KLERROR,VOID,ENERGY
C 3,RAND1,RAND,CON2,2B,10P,N,EMPTY,ISCUML,AVECOS,COSTHE
C DIMENSION SPACE(12598),IMAX(12),I1(12),A(12),REG(15,12),BLANK(31)
C 1,VOID(7505),REGD(12),IPMT1(12),IPMT2(12),ECUT(20),ECUT(12)
C 2,AVTCOS(20),SUMCOS(20),SUMCOS(20),SUMI(20),EMPIY(15,16,20)

C INITIALIZE
DO 99 ISLB=1,NI
  SUMCOS(IISLB)=0.
  SUMI(IISLB)=0.

99 CONTINUE
  ICP = 10P
  ENPV=0.
  NHIST=0.
  THIST=0.
  CURE=1./3.
  CON1=1.3977649E-03
  CON2=4.80286E-04
  HISTORY COUNTER
  1 NHIST=NHIST+1
  1 SUB=1
  TUT=0.
  J=1
  SUM=TMAX(J)
  IF(NHIST-NHIST)12,2,3
  1 INITIAL ENERGY
  2 IF(SLECTE-SPCFY)4,5,4
  5 ENERGY=EINT
  GO TO 55
  1 INITIAL ENERGY FROM FISSION SPECTRUM
  C AT PRESENT NOT AVAILABLE
  4 CALL FISS
  C FIND RANGE AND DEX FOR ENERGY
  55 CALL RAND(ENERGY,RE,DEX,J)
  C ANGLE OF INCIDENCE
  56 IF(SLECTA-SPCFY)6,61,6
  61 COSINE=COSFITHINT*0.0174533
  C THETA=THINT*0.0174533
  62 GO TO 121
  C FROM ISOTROPIC DISTRIBUTION
  6 CALL RAND
  C COSINE=RAND
  C THETA=ACOS(COSINE)
  121 XZU=CON1*(J)*2*A(J)*LOGF((183./IZ(J))*CUBE))
  121 GUTC(1004,1005),10P
  1004 DELT=FACTOR
  1005 DELT = FACTR/ENERGY
  1006 T=DELT*XZRO

```

## SUBROUTINE ELMC

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```

TEST=DELT*I*COSINE
TTOT=TTOT+TEST
C TEST TO DETERMINE WHICH SLAB ELECTRON IS NOW IN
C IF(TTOT-SUM)10 13,223,223
C 15 NOT IN SLAB J+1
1013 J=TTOT-(SUM-TMAX(J))222,222,134
C THE ELECTRON WENT TO SLAB J+1, SO LOCATE IT NOW
C AT THE BOUNDARY BETWEEN
C N=1
223 N=1
DELT=(SUM-1(TOT-TEST))/COSINE
T=DELT*XZRD
TTOT=SUM
SUM=SUM+TMAX(J+1)
1(FIDELT)227,226,227
227 IREG=REGNO(J)
GO TO 17
C THE ELECTRON BACKSCATTERED TO SLAB J-1
C IF TOTAL Z IS NEGATIVE THE ELECTRON BACKSCATTERED
C OUT FRONT OF THE SHIELD
222 I(FIDOT)116,16,225
C STILL IN SHIELD
225 N=3
SUM=SUM-TMAX(J)
DELT=(1(TOT-TEST))-SUM)/ABS(F(COSINE))
TTOT=SUM
1(FIDELT)228,226,228
228 IREG=1
T=DELT*XZRD
GO TO 17
16 I(FOPTION-BREM)1002,1,1002
1002 ISLB=N
CALL TRANS(THETA,ISLB)
IF(KEKAK)66,66,67
67 RETURN
68 CUSTHE=COSTHE
1(FCOSTHE)1,666,666
666 SUMCOSISLB)=SUMCOSISLB)+COSTHE
SUMISLB)=SUMISLB)+1.
GO TO 1
C HE ELECTRON IS STILL IN THE SAME SLAB
134 N=2
1END=RGENC(J)
DC 100 1,1,1END
1(FIDUR-REG)1,1,171,171,100
100 COMPUTE RADIATION LOSS
C 171 1DE=1
17 1(FIDUR-ZBISLB)1010,1011,1011
1C11 1(FOPTION-BREM)1014,1,1014
1014 CALL TRANS(THETA,ISLB)
CUSTHE=COSTHE
IF (CUSTHE) 2666, 3666, 3666
3666 SUMCOSISLB)=SUMCOSISLB)+COSTHE
SUMISLB)=SUMISLB)+1.

```

## SUBROUTINE ELMC

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2666 IF(LSLB-N)1666,1,1
1666 LSLB=LSLB+1
      GO TO 17
1010 CALL KADLCS
      IF(KRAD)<6.68,172
      TALLY RADIATION LOSS
      C 172 IF(OPTION-1KA)1722,68,1722
      1722 CALL ILYAC(IIFG,J)
      IF(KEKCK)68,69,69
      69 RETURN
      C COMPUTE IONIZATION LOSS
      68 EIO=DELT*DLDX
      C ENERGY FOR MOLLIKE CALCULATION
      C LMUL=ENERGY-(EION*ERAD)/2.
      C COMPUTE NEW ENERGY
      771 ENERGY=ENERGY-EION-ERAD
      IF(ENERGY-ECUT1(J))1,1,77
      COMPUTE SCATTER ANGLE
      C 77 CALL MULL1(J)
      IF(KEKUR)70,70,71
      71 RETURN
      70 CALL RANDM
      CHI=2.*3.14159*RAVD
      COSINE=COSINE*COSF(THTSCT)+COSF(CHI)*SINF(THTSCT)*SINF(THTSCT)-COSINE
      1*2)
996 THETA=Aacosf(CUSINt)
      276 GU TO (18,19,20),N
      20 J = J-1
      GO TO 19
      18 J=J+1
      19 CALL RANDF (ENERGY,RE,DEDX,J)
      GC TO 121
      3 DO 199 ISLB=1,N
      AVECOS(LSLB)=SUMCUS(LSLB)/SUM(LSLB)
      199 CONTINUE
      RETURN
      END,0,0,1,0,0,0,0,1,0,0,0,0,0,0,0,0

```

## SUBROUTINE TO OUTPUT ELECTRON MONTE CARLO

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```

SUBROUTINE OUT
COMMON SPACL,DISCPT,ECUT,IMAX,BLANK,REG,TPMT1,TPMT2,REGNO,ENGY,
IANGLE,NOSLAB,NOMIST,SLCT1,SPCFY,EINT,SLCT1,THINT,
2OPT1,BREM,FACTOR,TRA,BOIN,L1,L2,VOID,KERROR,NANI,IRDL,ALSD,IB8,10P,
3N1,FNEE,ISUM,AVECOS,COSTHE
DIMENSION SPACE(12586),DISCPT(112),BLANK(24),TPMT1
1,(12),TPMT2(12),REGNO(12),ENGY(15),ANGLE(16),NANT(15,16,20),IRDL(15
2,12,15),VOID(17),ALSO(9),ZB(20),KSUM(16),FNEE(15,16,20),REG(15,12)
3,ECUT(12),HEAD(16),HEAD(16),FSUM(16),AVECOS(120)
1CP = 10P
1SCUM=ISUM+NOMIST
DC 400 I=1,L2
HEAD(1)=1HN
HEAD(11)=1HE
400 WRITE PROBLEM DESCRIPTION
      WRITEOUTPUTTAPE6*10,(DISCPT(11),I=1,12),ISUM
      10 FORMAT(1H1,10X,12A6,3X,110,3H1STCH(2,7))
      IF(UPT1-BRF=12+1,2,
      2 WRITEOUTPUTTAPE6*20
      20 FORMAT(1H ,37X,4.6HELECTRON MONTE CARLO TRANSMISSION DISTRIBUTION//)
1)

GOTO3
1 WRITE OUTPUT TAPE6,30
30 FORMAT(1H ,32X,5SH ELECTRON MONTE CARLO RADIATION ENERGY LOSS DISTR
IBUTION//)
3 IF(SLCT1-SPCFY)14,5,4
5 WRITEOUTPUTTAPE6*40,EINT
40 FORMAT(32H INITIAL ENERGY SPECIFIED TO BE 1PE15.6,5H MEV,//)
GOTG6
4 WRITEOUTPUTTAPE6*50
50 FORMAT(57H INITIAL ENERGY DETERMINED FROM FISSION ELECTRON SPECTRU
M//)
6 IF(SLCT1-SPCFY)7,8,7
8 WRITEOUTPUTTAPE6,63,THINT
60 FORMAT(44H INITIAL ANGLE OF INCIDENCE SPECIFIED TO BE 1PE15.6,8H D
IEGKES//)
GOTG9
7 WRITE OUTPUT TAPE 6,70
70 FORMAT(6H INITIAL ANGLE OF INCIDENCE DETERMINED FROM ISOTROPIC DI
STRIBUTION//)
9 GOTO (111,112),10P
111 WRITE OUTPUT TAPE 6, 113, FACTOK
113 FORMAT(9H CELIA T=F7.4//)
114 IC 116
112 WRITE OUTPUT TAPE 6, 114, FACTOK
114 FORMAT(12H DELTA T=F7.4,7H/E ENERGY//)
116 WRITE OUT PUTTAPE6,80,NOSLAB
80 FORMAT(14H SHIFT CONSISTS OF 110,6H SLABS//)
81,100 WRITEOUTPUTTAPE6,110,J,TPMT1(J),TPMT2(J),TMX1(J)
115 FORMAT(5H SLAB13,4H IS 246,13H OF THICKNESS TP15.6,10H GM./CM**2)
C TEST FOR OUTPUT ARRAY = ANTED
115 IF (OPT1-NREM) 117, 17, 117

```

## SUBROUTINE TO OUTPUT ELECTRON MOVE CAHLO

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117 IF (NI-1) 118, 13, 119
118 KERON = 12
      RETURN
119 WRITE OUTPUT TAPE 6, 121, NI
121 FORMAT(32H TRANSMISSION DISTRIBUTIONS FOR 13.6H CASES//)
DO 122 I=1, NI
122 WRITE OUTPUT TAPE 6, 123, I, 2BC(I)
123 FORMAT(1H CASE13,2H IS A SLAB OF THICKNESS PE15.6,10H GM./CM.//2//)
1)
      WRITE TRANSMISSION ARRAY
C   13 DO 1004 ISLB=1,NI
      LM1=1
      LM2=5
      KTRANS=1
      WRITE OUTPUT TAPE 6,1334,ISLB,ZB((ISLB))
1334 FORMAT(15H0 TRANSMISSION DISTRIBUTION FOR CASE14,24H WITH SLAB OF T
1HICKNESS 1PE15.6,10H GM./CM.//2//)
1444 IF(LM2-LM1)14,14,16
14 LM2=L2
      KTRANS=2
16 WRITE OUTPUT TAPE 6,120,(ANGLE(I),I=LM1,LM2)
120 FORMAT(1H,50X,18M TRANSMISSION ANGLE/1H,15X,5(F6.2,12X)//)
      WRITE OUTPUT TAPE 6,160,(HEADN(I),HEADE(I),I=LM1,LM2)
160 FORMAT(7H ENERGY,7X,10(A6,3X)//)
DC200=1,L1
200 WRITE OUTPUT TAPE 6,130,ENGY(I),INANT(I,J,ISLB),FNEE(I,J,ISLB),LM1,
1LM2)
130 FORMAT(1H ,F6.3,4X,S(16,2X,F 8.2,2X))
      DG 211 J=LM1, LM2
      FSUM(J)=0.
      KSUM(J)=0
      KSUM(J)=0
      DU 212 I=1, L1
      FSUM(J)=FSUM(J)+FHEE(I,J,ISLB)
212 KSUM(J)= KSUM(J)+NANT(I,J,ISLB)
211 CONTINUE
      WRITE OUTPUT TAPE 6, 216, (KSUM(J),FSUM(J),J=LM1,LM2)
216 FORMAT(7H TOTALS,4X,S(16,2X,F8.2,2X))
      GO TO 115, 213,KTRANS
15 LM1=LM1+5
      LM2=LM2+5
      GU TO 1444
213 ISUM = 0
      DU 214 J=1, L2
214 ISUM = ISUM+KSUM(J)
      WRITE OUTPUT TAPE 6, 215, ISUM
215 FORMAT(21H TOTAL TRANSMITTED = 110)
1004 CONTINUE
      WRITE OUTPUT TAPE 6, 99
99 FORMAT(1H0,45X,31H AVERAGE TRANSMISSION COSINES//2115X,10MTHICKN
1ESS ,15X,10H COSINE *10X)
      WRITE OUTPUT TAPE 6,994,(ZRH(I),AVECCS(I),I=1,11)
999 FORMAT(21L0X,F15.6,10X,E15.6,10X)
      IF(UPI-BCLH)11,25,11
      WRITE OUTPUT TAPE 6,30
25

```

## SUBROUTINE TO OUTPUT ELECTRON MONTE CARLO

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```

C   WRITE RADIATION ENERGY LOSS ARRAY
      17  DO21J=1,NCSLAB
          LM2=6
          LM1=1
          KTRANS=1
      26  IF(LI)-LM2 118,18,22
      18  LM2=LI
          KTRANS=2
          GOT022
      22  WRITEOUTPUTAPE6,140,(ENGY(I),I=LM1,LM2)
      140  FORMAT(53X,13HENERGY (MEV.),//7H REGION,4X,6(F6.3,7X)//)
          NUREG=REGNO(I,J)
          DC3001=1,NUREG
      300  WRITEDOUTPUTAPE6,150,I,(IRDL(I,J,K),K=LM1,LM2)
      150  FORMAT(1H ,16,4X,B(16,7X))
          GO TO 127,21),KTRANS
      27  LM1=LM1+6
          LM2=LM2+6
          GO TO 26
      21  CONTINUE
      11  RETURN
      END(1,0,0,1,0,0,0,0,1,0,0,0,0,0,0,0)

```

## SUBROUTINE TRANSITHT(ISTB)

```

SUBROUTINE TRANSITHT(ISTB)
COMMON BLANK,ENGY,ANGLE,SPACE,L1,L2,VOID,KTRKOK,NANT,ALSO,ENERGY
1,100,FNEE,J,SCUM,AVFCUS,COS1,HE
DIMENSION BLANK(12862),ENGY(15),ANGLE(16),SPACE(12),VOID(7),
NANT(15,16,20),ALSO(27051),100(251),FNEE(15,16,20),AVECOS(20),
100-1SLB
100-1SLB
      TH=THT
      COS TH=COSF(TH)
      THE1A=THT-.57.296
      5 IF (THE1A-3.60.-) 3, 4, 4
      4 THE1A = THE1A-360.
      GO TO 5
      3 DC 100 1=1,L1
      IF(ENERGY-ENGY(1)) 1,1,100
      100 CONTINUE
      KERROR=5
      RETURN
      1 DO 200 J=1,L2
      1 IF (THE1A-ANGLE(J)) 2,2,200
      200 CONTINUE
      KERROR=4
      RETURN
      2 NANT(J,J,IGC)=NANT(1,J,IGD)+1
      FNEE(1,J,IGD)=FNEE(1,J,IGD)+ENERGY
      RETURN
      END1,0,0,1,0,0,0,0,1,0,0,0,0,0,0,0,0,0

```

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## SUBROUTINE MOLLIJ(SLAB)

```

SUBROUTINE MOLLIJ(SLAB)
COMMON BLANK,Z,A,SPACE,FACTOR,EMPTY,THTSCT,T,CUBE,ENOL,DELT,
IERRK0,VOID,DEN,SMLB,BBIG,CHIC,VALUE,EN,RAND,CON2
DIMENSION BLANK(26221),Z(12),A(12),SPACE(256),VOID(7500),EMPTY(6)
J=JSLAB
BETSO=1.-(.51/(EMCL+.51))**2
SMLB=LLOGF(6680.*DELT*(Z(J)+1.)*Z(J)*CURE/(BETSO*A(J+1)+.51))
10 Z(J)=2*(1.+4.*EMOL*(EMOL+1.)/(EMOL*(EMOL+1.)))
IF(SMLB<-1.)3,4,4
3 IF(DELTA-FACTOR)>10,20,20
10 THTSCT=0.
      RETURN
20 KERKOK=2
      RETURN
      FIND BBIG SUCH THAT  $\text{BBIG} = \text{LN}(\text{BBIG}) - \text{SMLB}$ 
      C   4 CALL DETB
      1 IF(KERKOK) 1,1,2
      2 RETURN
      1 CHIC=SORTF(CON2=25.+7089E-05*DELT*(Z(J)+1.)*(A(J)+.51))
      1 IF(DELTA=.21)
      1 FIND INTEGRAL FROM Q TO 2*PI/(CHIC*BBIG*.1/2)
      C   CALL DENOM
      C   FIND RANDM NUMBER
      CALL RANDP
      VALUE=RAND*DEN
      C   FIND UPPER LIMIT OF INTEGRA EQUAL TO VALUE
      CALL NUM
      RETURN
      END(1.0,0.1,0.0,0.0,0.1,0.0,0.0,0.0)

```

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#### **SUBROUTINE DETA**

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A

SUGAR OUTLINE TLYRD (IREG: JSLAB)

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## SUBROUTINE DENOM

```

COMMON BLANK,DUM1,UPLIM,DUM2,FZINT,DUM3,FINT,DUM4,
1F2INT,SPACE,DEV,SMLB,BBIG,CHIC
DIMENSION BLANK(2070),UPLIM(128),FZINT(128),FINT(128),
1F2INT(128),SPACE( 7829)
XU=3.14159/(CHIC*SQRT(BBIG))
IF(XU<9.3)13,4,4
4 DEN=1.-.0118416/BBIG+.041235/(BBIG**2)
      RETURN
3 DO 100 I=1,93
     IF(XU-UPLIM(I)) 1,2,100
100 CONTINUE
      RETURN
2 DEN=FZINT(I)*FINT(I)/BBIG+F2INT(I)/(BBIG**2)
      RETURN
1 CCNST=(UPLIM(I-1)-XU)/(UPLIM(I-1)-UPLIM(I))
      FZRO=CONST*(FZINT(I-1)-F2INT(I-1)+F2INT(I-1))
      FONE=CONST*(F1INT(I-1)-F1INT(I-1)+F1INT(I-1))
      FIWO=CONST*(F2INT(I-1)-F2INT(I-1)+F2INT(I-1))
      DEN=FZRO+FONE/BBIG+FIWO/(BBIG**2)
      RETURN
END(1,0,0,1,0,0,0,0,1,0,0,0,0,0,0,0)
```

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	ENTRY	NUM	
TRANSFER VECTOR			
00000 625051636060	SORT		
LINKAGE DIRECTOR			
00001 000000000000			
00002 456444606060			
00003 -0634 00 4 00001	NUM	NUM-2,4	
00004 0634 09 1 00001	SXD	SXA	
00005 0774 00 1 00000	AXT	0,1	
00006 -0560 00 0 53200	LDQ	B	
00007 0260 00 0 23200	FMP	H	
00010 0601 00 0 00252	STU	BSQ	
00011 0500 00 1 72531	CLA	F2INT+1-64,1	
00012 0601 00 0 00250	STO	TEMP	
00013 0241 00 0 00252	FDP	BSQ	
00014 -0600 00 0 00250	STQ	TEMP	
00015 0500 00 1 72732	CLA	F1INT+1-64,1	
00016 0241 00 0 53200	FDP	B	
00017 0131 00 0 00000	XCA		
00020 0300 00 0 00250	FAD	TEMP	
00021 0300 00 1 73133	FAD	F2INT+1-64,1	
00022 0601 00 0 00250	STU	TEMP	
00023 0500 00 0 53176	CLA	VALUE	
00024 0340 00 0 00250	CAS	TEMP	
00025 1 00100 1 00077	TXI	*+2,1,64	
00026 0020 00 0 00077	TRA	*+1	
00027 0500 00 1 72571	CLA	F2INT+1-64+32,1	
00030 0601 00 0 00250	STO	TEMP	
00031 0241 00 0 00252	FDP	BSQ	
00032 -0600 00 0 00250	SIQ	TEMP	
00033 0500 00 1 72772	CLA	F1INT+1-64+32,1	
00034 0241 00 0 53200	FDP	B	
00035 0131 00 0 00000	XCA		
00036 0300 00 0 00250	FAD	TEMP	
00037 0300 00 1 73173	FAD	F2INT+1-64+32,1	
00040 0601 00 0 00250	STO	TEMP	
00041 0500 00 0 53176	CLA	VALUE	
00042 0340 00 0 00250	CAS	TEMP	
00043 1 00040 1 00045	TXI	*+2,1,32	
00044 0020 00 0 00045	TRA	*+1	
00045 0500 00 1 72611	CLA	F2INT+1-64+32+16,1	
00046 0601 00 0 00250	STO	TEMP	
00047 0241 00 0 00252	FDP	BSQ	
00050 -0600 00 0 00250	STO	TEMP	
00051 0500 00 1 73012	CLA	F1INT+1-64+32+16,1	
00052 0241 00 0 53200	FDP	B	
00053 0131 00 0 00070	XCA		
00054 0300 00 0 00250	FAD	TEMP	
00055 0300 00 1 73213	FAD	F2INT+1-64+32+16,1	
00056 0601 00 0 00250	STO	TEMP	
00057 0500 00 0 53176	CLA	VALUE	

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00060 0340 00 00250   CAS TEMP
    00061 1 00020 1 00063   TX1 *+2,1,16
    00062 0020 00 0 00063   TRA *+1
    00063 0500 00 1 72621   CLA F2INT+1-64+32+16+8,1
    00064 0601 00 0 00250   STD TEMP
    00065 0241 00 0 00252   FDP BSQ
    00066 -0600 00 0 00250   STO TEMP
    00067 0500 00 1 73022   CLA F2INT+1-64+32+16+8,1
    00070 0241 00 0 53200   FDP B
    00071 0131 00 0 00030   XCA
    00072 0300 00 0 00250   FAD TEMP
    00073 0300 00 1 73223   FAD F2INT+1-64+32+16+8,1
    00074 0601 00 0 00250   STO TEMP
    00075 0500 00 0 53176   CLA VALUE
    00076 0340 00 0 00250   CAS TEMP
    00077 1 00010 1 00101   TX1 *+2,1,8
    00100 0020 00 0 00101   TRA *+1
    00101 0500 00 1 72625   CLA F2INT+1-64+32+16+8+4,1
    00102 0601 00 0 00250   STO TEMP
    00103 0241 00 0 00252   FDP BSQ
    00104 -0600 00 0 00250   STQ TEMP
    00105 0500 00 1 73026   CLA F2INT+1-64+32+16+8+4,1
    00106 0241 00 0 53200   FDP B
    00107 0131 00 0 00030   XCA
    00110 0300 00 0 00250   FAD TEMP
    00111 0300 00 1 73227   FAD F2INT+1-64+32+16+8+4,1
    00112 0601 00 0 00250   STO TEMP
    00113 0500 00 0 53176   CLA VALUE
    00114 0340 00 0 00250   CAS TEMP
    00115 1 00004 1 00117   TX1 *+2,1,4
    00116 0020 00 0 00117   TRA *+1
    00117 0500 00 1 72627   CLA F2INT+1-64+32+16+8+4+2,1
    00120 0601 00 0 00250   STO TEMP
    00121 0241 00 0 00252   FDP BSQ
    00122 -0600 00 0 00250   STQ TEMP
    00123 0500 00 1 73030   CLA F2INT+1-64+32+16+8+4+2,1
    00124 0241 00 0 53200   FDP B
    00125 0131 00 0 00030   XCA
    00126 0300 00 0 00250   FAD TEMP
    00127 0100 00 1 73231   FAD F2INT+1-64+32+16+8+4+2,1
    00128 0601 00 0 00250   STO TEMP
    00131 0500 00 0 53176   CLA VALUE
    00132 0340 00 0 00250   CAS TEMP
    00133 1 00002 1 00135   TX1 *+2,1,2
    00134 0020 00 0 00135   IRA *+1
    00135 0500 00 1 72630   CLA F2INT+1-64+32+16+8+4+2,1
    00136 0601 00 0 00250   STO TEMP
    00137 0241 00 0 00252   FDP BSQ
    00140 -0600 00 0 00250   STQ TEMP
    00141 0500 00 1 73031   CLA F2INT+1-64+32+16+8+4+2+1,1
    00142 0241 00 0 53200   FDP B
    00143 0131 00 0 00030   XCA
    00144 0300 00 0 00250   FAD TEMP
    00145 0300 00 1 73232   FAD F2INT+1-64+32+16+8+4+2+1,1

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	TEMP	STO	CLA	F2INT-1,1	
	VALUE	STO	CAS	TEMP	
	TEMP	TRA	LESS	TEMP	
	LESS	TRA	OUT	TEMP	
	GREAT	TRA	TEMP	F2INT-1,1	
00146	0601 00 0 00250				
00147	0500 00 0 53176	STO	CLA		
00150	0340 00 0 00250		CAS		
00151	C020 00 0 00154		TRA		
00152	C020 00 0 00233		TRA		
00153	0020 00 0 00204		TRA		
00154	0500 00 1 72627	LESS	CLA		
00155	0601 00 0 00251		STO	TEMP1	
00156	0241 00 0 00252		FDP	BSQ	
00157	-0600 00 0 00251		STO	TEMP1	
00160	0500 00 1 73030		CLA	FLINT-1,1	
00161	0241 00 0 53200		FDP	B	
00162	0131 00 0 00000		XCA		
00163	0300 00 0 00251		FAD	TEMP1	
00164	0300 00 1 73231		FAD	F2INI-1,1	
00165	0601 00 0 00251		STO	TEMP1	
00166	-0760 00 0 00003		SSM		
00167	0300 00 0 00250		FAD	TEMP	
00170	0601 00 0 00253		STO	TEST1	
00171	0500 00 0 00250		CLA	TEMP	
00172	0302 00 0 53176		FSB	VALUE	
00173	0601 00 0 00250		STO	TEMP	
00174	0500 00 1 73433		CLA	UPLIM,1	
00175	0302 00 1 73432		FSB	UPLIM-1,1	
00176	0241 00 0 00253		FDP	TEST1	
00177	0260 00 0 00250		FMP	TEMP	
00200	0760 00 0 00003		SSP		
00201	0300 00 1 73433		FAD	UPLIM,1	
00202	0601 00 0 00247		STO	ETA	
00203	0020 00 0 00235		TRA	OUT1	
00204	0500 00 1 72631		CLA	F2INI+1,1	
00205	0601 00 0 00251		STO	TEMP1	
00206	0241 00 0 00252		FDP	BSQ	
00207	-0600 00 0 00251		STO	TEMP1	
00210	0500 00 1 73032		CLA	F2INI+1,1	
00211	0241 00 0 53200		FDP	B	
00212	0131 00 0 00000		XCA		
00213	0300 00 0 00251		FAD	TEMP1	
00214	0300 00 1 73233		FAD	F2INI+1,1	
00215	0601 00 0 00251		STO	TEMP1	
00216	0302 00 0 00250		FSB	TEMP	
00217	0601 00 0 00253		STO	TEST1	
00220	0500 00 0 00251		CLA	TEMP1	
00221	0302 00 0 53176		FSB	VALUE	
00222	0601 00 0 00250		STO	TEMP	
00223	0500 00 1 73434		CLA	UPLIM+1,1	
00224	0302 00 1 73433		FSB	UPLIM,1	
00225	0241 00 0 00253		FDP	TEST1	
00226	0260 00 0 00250		FMP	TEMP	
00227	0760 00 0 00003		SSP		
00230	0300 00 1 73434		FAD		
00231	0601 00 0 00247		STO	ETA	
00232	0020 00 0 00235		TRA	OUT1	
00233	0500 00 1 73433		CLA	UPLIM,1	

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00234	0601	00	0	00247	STO	ETA
00235	0500	00	0	53200	CLA	B
00236	0074	00	4	00000	TSX	\$5071.4
00237	0131	00	0	00000	XCA	
00240	0260	00	0	53177	FMP	CHIC
00241	0131	00	0	00000	XCA	
00242	0260	00	0	00247	FMP	ETA
00243	0601	00	0	71724	STO	THTSCT
00244	-0534	00	4	00001	LXD	NUM-2.4
00245	0534	00	1	00001	LXA	NUM-2.1
00246	0020	00	4	00001	TRA	1.4
00247	0	00000	0	00000	ETA	PZ
00250	0	00000	0	00000	TEMP	PZ
00251	0	00000	0	00000	TEMP1	PZ
00252	0	00000	0	00000	B5Q	PZ
00253	0	00000	0	00000	TEST1	PZ
				73433	UPLIM	COMMON
				73232	FLINT	COMMON
				73031	FLINT	COMMON
				72630	FLINT	COMMON
				71724	THTSCT	COMMON
				53200	COMMON	1
				53200	B	COMMON
				53177	CHIC	COMMON
				53176	VALUE	COMMON
					END	

	TRANSFER VECTOR	ENTRY	RADLOS
00000	512145244460	RANDOM	
00001	256747606060	EXP	
LINKAGE DIRECTOR			
00002	000000000000		
00003	512124434662		
00004	-0634 00 4	00002	RADLOS SXD
00005	0634 00 1	00002	SXA
00006	0774 00 1	00000	AXT
00007	0074 00 4	00000	TSX
00010	C241 00 0	71723	SHANDM,4
00011	0260 00 0	00114	FDP
00012	0601 00 0	00110	FMP
00013	0302 00 0	00115	EUNE
00014	0120 00 0	00106	STD
00015	0500 00 0	00110	FSB
00016	0302 00 0	00113	=24.75
00017	-0120 00 0	00103	OUTI
00020	0500 00 0	00110	TPL
00021	0340 00 1	73736	CLA
00022	1 00100 1	00024	EUNE
00023	0020 00 0	00024	FSB
00024	0340 00 1	73776	=1.66134E-10
00025	1 00040 1	00027	TM1
00026	0020 00 0	00027	EDNE
00027	0340 00 1	74016	CAS
00030	1 00020 1	00032	TXI
00031	0020 00 0	00032	TRA
00032	0340 00 1	74026	CAS
00033	1 00010 1	00035	TXI
00034	0020 00 0	00035	TRA
00035	0340 00 1	74032	CAS
00036	1 00004 1	00040	TXI
00037	0020 00 0	00040	TRA
00040	0340 00 1	74034	CAS
00041	1 00002 1	00043	TXI
00042	0020 00 0	00043	TRA
00043	0340 00 1	74035	CAS
00044	1 00001 1	00046	TXI
00045	0020 00 0	00046	TRA
00046	0302 00 1	74035	CAS
00047	-C120 00 0	00051	TXI
00050	1 00001 1	00051	TRA
00051	C700 00 1	74036	CAS
00052	0302 00 1	74035	TXA
00053	C601 00 0	00112	FSB
00054	C500 00 1	74036	TEMPI
00055	0302 00 0	00110	FSB
00056	0241 00 0	00112	FDP
00057	-0600 00 0	00112	TEMPI

	ARG+1,1		ARG,1	
00060	0500	00 1	73635	CLA
00061	0302	00 1	73634	FSB
00062	0131	00 0	00000	XCA
00063	0260	00 0	00112	TEMP1
00064	-0760	00 0	00003	FMP
00065	0300	00 1	73635	SSM
00066	-0760	00 0	00003	FAD
00067	0074	00 4	00001	SSM
00070	1 00000	0	00072	CALL EXP
00071	0 00103	0	00002	XCA
00072	0131	00 0	00000	FMP ENERGY
00073	0260	00 0	53175	STO X
00074	0601	00 0	00111	CLA ENERGY
00075	0500	00 0	53175	FSB X
00076	0302	00 0	00111	ERAD
00077	0601	00 0	71725	STO RADLOSS-2,4
00100	-0534	00 4	00002	OUT LXD
00101	0534	00 1	00002	LXA RADLOSS-2,1
00102	0020	00 4	00001	TRA 1,4
00103	0500	00 0	53175	OUT2 CLA ENERGY
00104	0601	00 0	71725	STO ERAD
00105	0020	00 0	00100	TRA OUT
00106	0600	00 0	71725	OUT1 STZ ERAD
00107	0020	00 0	00100	TRA OUT
00110	0 00000	0 00000	EONE PZE	
00111	0 00000	0 00000	X PZE	
00112	0 00000	0 00000	TEMP1 PZE	
	74035		COMMON 1812	
	74035		E1 COMMON 129	
	73634		ARG COMMON 129	
	71725		COMMON 838	
	71725		ERAD COMMON 1	
	71723		COMMON 1	
	71723	T	COMMON 1	
	53175		COMMON 7509	
	53175		ENERGY COMMON 1	
			END	

## LITERALS

00113 1405552202  
 00114 200542711072  
 00115 205614000000

## **SAMPLE INPUT DATA**

## DATA

```

*   9•950166-34•136190-3•011404   •2   3•921056-21•547448-2•043951
*   8•606881-23•101783-2•088491   •4   1•478562-14•643744-2•133684
*   2•211992-15•692073-2•168174   •6   3•C23236-15•809404-2•181999
*   3•873735-14•683330-2•165999   •8   4•727075-12•181006-2•126374
*   5•551419-1-1•63142-2•071999   1•   6•321205-1-6•50541-2•009599
*   7•018028-1-1•20562-1-•049426   1•2   7•630723-1-1•78269-1-•045551
*   8•154807-1-2•33574-1-•073176   1•4   8•591419-1-2•82450-1-•078199
*   8•946011-1-3•21884-1-•059612   1•6   9•226957-1-3•50098-1-•026362
*   9•444243-1-3•66567-1•013638   1•8   9•608367-1-3•71856-1•056123
*   9•729488-1-3•67356-1•095485   2•0   9•816851-1-3•54961-1•12669
*   2•1   9•878456-1-3•36769-1•14802   2•2   9•920937-1-3•14825-1•160848
*   2•3   9•949590-1-2•90939-1•160236   2•4   9•968497-1-2•66587-1•151884
*   2•5   9•880704-1-2•42865-1•138582   2•6   9•988416-1-2•20531-1•122614
*   2•7   9•993185-1-2•00008-1•105696   2•8   9•996071-1-1•81494-1•089574
*   2•9   9•997782-1-1•65006-1•075352   3•0   9•998774-1-1•50443-1•063376
*   3•1   9•993337-1-1•37641-1•053875   3•2   9•999651-1-1•26403-1•046662
*   3•3   9•999821-1-1•16530-1•041625   3•4   9•999912-1-1•07834-1•038154
*   3•5   9•999960-1-1•00144-1•036059   3•6   9•999984-1-2•33119-2•034946
*   3•7   9•999996-1-8•72128-2•034238   3•8   1•   -8•17408-2•034005
*   3•9   1•   -7•68080-2•034129   4•0   1•   000001   -7•23411-2•034466
*   4•1   1•000001   -6•82793-2•034909   4•2   1•   000001   -6•45717-2•035386
*   4•3   1•000001   -6•11756-2•035891   4•4   1•   000001   -5•80548-2•036422
*   4•5   1•00001   -5•51788-2•036971   4•6   1•   000001   -5•25212-2•037516
*   4•7   1•00001   -5•00593-2•038039   4•8   1•   000001   -4•77735-2•038532
*   4•9   1•000001   -4•56466-2•03899   5•   1•   000001   -4•36637-2•039417
*   5•1   1•000001   -4•18116-2•039814   5•2   1•   000001   -4•00787-2•04018325
*   5•3   1•000001   -3•84545-2•040462   5•4   1•   000001   -3•69299-2•040777
*   5•5   1•000001   -3•54968-2•041075   5•6   1•   000001   -3•41476-2•041352
*   5•7   1•000001   -3•28758-2•041612   5•8   1•   000001   -3•16755-2•041855
*   5•9   1•000001   -3•05412-2•042081   6•0   1•   000001   -2•94682-2•04229
*   6•1   1•000001   -2•84519-2•04248975   6•2   1•   000001   -2•74883-2•042675
*   6•3   1•000001   -2•65739-2•0428466   6•4   1•   000001   -2•57052-2•0430066
*   6•5   1•000001   -2•48792-2•043159   6•6   1•   000001   -2•4930-2•0433029
*   6•7   1•000001   -2•3442-2•0434366   6•8   1•   000001   -2•26303-2•0435629
*   6•9   1•000001   -2•19492-2•0436804   7•0   1•   000001   -2•12989-2•043789
*   7•1   1•000001   -2•06774-2•0438916   7•2   1•   000001   -2•00832-2•0439854
*   7•3   1•000001   -1•95145-2•044074   7•4   1•   000001   -1•89700-2•0441579
*   7•5   1•000001   -1•84483-2•0442366   7•6   1•   000001   -1•79481-2•0443104
*   7•7   1•000001   -1•74663-2•0443816   7•8   1•   000001   -1•70076-2•044479

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10.7      1.939263-610.5      2.410323-610.3      2.996747-6  
 10.1      3.727057-69.9      4.636905-69.7      5.770885-6  
 9.5      7.184799-69.3      8.948516-69.1      1.114958-5  
 8.9      1.389772-58.7      1.733064-58.5      2.162117-5  
 8.3      2.698647-58.1      3.369957-57.9      4.210407-5  
 7.7      5.263270-57.5      6.583100-57.3      8.238736-5  
 7.1      1.031714-46.9      1.292828-46.7      1.621140-4  
 6.5      2.034301-46.3      2.554717-46.1      3.210873-4  
 5.9      4.039038-45.7      5.085468-45.5      6.409264-4  
 5.3      8.086087-45.1      1.021300-34.9      1.291484-3  
 4.7      1.635249-34.5      2.073400-34.3      2.632911-3  
 4.1      3.348879-33.9      4.267142-33.7      5.447820-3  
 3.5      6.970133-33.3      8.939031-33.1      1.149440-2  
 2.9      1.482399-22.7      1.918183-22.5      2.491484-2  
 2.3      3.250214-22.1      4.261413-21.9      5.620402-2  
 1.7      7.465402-21.5      1.000185-11.3      1.354488-1  
 1.1      1.859867-1.9      2.601839-1.7      3.737688-1  
 .5      5.597736-1.3      9.056767-1      1.11.822924  
 7.0      -22.150838      4.0-22.681264      1.-24.037930  
 7.0      -34.391617      4.0-34.948241      1.-36.331539  
 7.0      -46.687914      4.0-47.247230      1.-48.633225  
 7.0      -58.989869      4.0-59.549455      1.-51.093572+1  
 7.0      -61.129239+1      4.0-61.185200+1      1.-61.323830+1  
 7.0      -71.359497+1      4.0-71.415459+1      1.-71.554088+1  
 7.0      -81.589755+1      4.0-81.645717+1      1.-81.784346+1  
 7.0      -91.820014+1      4.0-91.875976+1      1.-92.014605+1  
 7.0      -102.050272+1      4.0-102.106234+1      1.-102.244863+1  
 7.0      -112.280531+1      4.0-112.336493+1      1.-112.4751122+1  
 ELECTRON MONTE CARLO FOR 3 MEV OF LEAD AND INITIAL ANGLE OF 0 DEG  
 SPECIFY BREMTRANS      1.      1000      1000

1. LEAD      1.6      15.      207.21      82.      .01  
 .8      2.1.6  
 .095      81536047153  
 25.      .01  
 0.      0.      0.  
 .00251      4.87      .03  
 .00497      3.78      .04  
 .000893      7.29      .02  
 .00778      .00778

3.16	•05	•0113	2.74	•06	•0151	2.45
•07	•0194	2.24	•08	•0240	2.07	•09
•0291	1.93	•10	•0343	1.82	•15	•0652
1.48	•20	•101	1.30	•25	•142	1.19
•30	•185	•1.13	•35	•230	1.08	•40
•277	1.04	•45	•326	1.02	•50	•375
1.00	•55	•426	•989	•60	•476	•979
•65	•528	•972	•70	•579	•966	•75
•631	•963	•80	•683	•960		
		10				
		•3	•6	•9	1.2	1.5
		2.4	2.7	3.		1.8
		7	30.	45.	60.	90.
		15.				180.

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### **SAMPLE PROBLEM**

ELECTRON MONTE CARLO FOR 3 MEV OF LEAD AND INITIAL ANGLE OF 0 DEG  
INITIAL ENERGY SPECIFIED TO BE 3.000000E 00 MEV.

INITIAL ANGLE OF INCIDENCE SPECIFIED TO BE 0.  
DEGREES

DELTA T = 0.0950

SHIELD CONSISTS OF 1 SLABS

SLAB 1 IS LEAD OF THICKNESS 1.600000E 00 GM./CM\*\*2  
TRANSMISSION DISTRIBUTIONS FOR 2 CASES

CASE 1 IS A SLAB OF THICKNESS 8.000000E-01 GM./CM\*\*2

CASE 2 IS A SLAB OF THICKNESS 1.600000E 00 GM./CM\*\*2

TRANSMISSION DISTRIBUTION FOR CASE 1 WITH SLAB OF THICKNESS 8.000000E-01 GM./CM\*\*2

ENERGY	TRANSMISSION ANGLE					
	15.00	30.00	45.00	60.00	75.00	90.00
0.300	4.073	5	0.83	7	1.25	3
0.600	0.44	3	1.59	5	2.85	5
0.900	3.16	7	5.02	4	2.93	6
1.200	5.50	3	3.05	6	6.43	6.15
1.500	6.834	14	18.15	10	13.35	13
1.800	5.00	9	15.02	11	17.70	20
2.100	17.80	19	36.79	31	61.08	20
2.400	6.13	17	36.84	7	14.99	6
2.700	0	0	0.	0.	0.	12.98
3.000	0	0	0.	0.	0.	10.80
TOTALS	.38	.54.13	.77	.117.30	.81	.120.59
					.83	.121.20
						.40
						<b>57.03</b>

ENERGY	TRANSMISSION ANGLE					
	15.00	30.00	45.00	60.00	75.00	90.00
0.300	1	0.05	0	0	0	0
0.600	1	0.57	0	0	0	0
0.900	1	0.66	0	0	0	0
1.200	1	1.06	0	0	0	0
1.500	1	1.46	0	0	0	0
1.800	3	5.13	0	0	0	0
2.100	6	11.77	0	0	0	0
2.400	0	0	0	0	0	0
2.700	0	0	0	0	0	0
3.000	C	0.	0.	0.	0.	0.
TOTALS						14.71

TOTAL TRANSMITTED = 333

TRANSMISSION DISTRIBUTION FOR CASE 2 WITH SLAB OF THICKNESS 1.60000E 00 GM./CM<sup>0.2</sup>

TRANSMISSION ANGLE

ENERGY	15.00			30.00			45.00			60.00			75.00		
	N	E	N	N	E	N	N	E	N	N	E	N	N	E	
0.300	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0.600	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0.900	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
1.200	1	0.96	0	0	0	0	0	0	0	0	0	0	0	0	0
1.500	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
1.800	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
2.100	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
2.400	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
2.700	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
3.000	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
TOTALS	1	0.96	0	0	0	0	0	0	0	0	0	0	0	0	0

TRANSMISSION ANGLE

ENERGY	90.00			180.00			270.00			360.00			450.00		
	N	E	N	N	E	N	N	E	N	N	E	N	N	E	
0.300	0	0	0	11	11	11	11	11	11	11	11	11	11	11	11
0.600	0	0	0	11	11	11	11	11	11	11	11	11	11	11	11
0.900	0	0	0	25	25	25	25	25	25	25	25	25	25	25	25
1.200	0	0	0	31	31	31	31	31	31	31	31	31	31	31	31
1.500	0	0	0	35	35	35	35	35	35	35	35	35	35	35	35
1.800	0	0	0	42	42	42	42	42	42	42	42	42	42	42	42
2.100	0	0	0	30	30	30	30	30	30	30	30	30	30	30	30
2.400	0	0	0	26	26	26	26	26	26	26	26	26	26	26	26
2.700	0	0	0	20	20	20	20	20	20	20	20	20	20	20	20
3.000	0	0	0	9	9	9	9	9	9	9	9	9	9	9	9
TOTALS	0	0	0	240	240	240	240	240	240	240	240	240	240	240	240

TOTAL TRANSMITTED = 243

AVERAGE TRANSMISSION COSINES

COSINE THICKNESS

0.660000E 00 0.723862E 00 0.16000E 01 ELECTRON MONTE CARLO RADIATION ENERGY LOSS DISTRIBUTION

ENERGY (MEV.)

THICKNESS		COSINE		THICKNESS		COSINE	
REGION	0.300	0.600	0.900	1.200	1.500	1.800	
1	723	33	15	5	3	4	
2	947	37	24	9	8	2	
3	1066	38	20	13	12	4	
4	1217	47	14	12	14	1	

REGION	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100	101	102	103	104	105	106	107	108	109	110	111	112	113	114	115	116	117	118	119	120	121	122	123	124	125	126	127	128	129	130	131	132	133	134	135	136	137	138	139	140	141	142	143	144	145	146	147	148	149	150	151	152	153	154	155	156	157	158	159	160	161	162	163	164	165	166	167	168	169	170	171	172	173	174	175	176	177	178	179	180	181	182	183	184	185	186	187	188	189	190	191	192	193	194	195	196	197	198	199	200	201	202	203	204	205	206	207	208	209	210	211	212	213	214	215	216	217	218	219	220	221	222	223	224	225	226	227	228	229	230	231	232	233	234	235	236	237	238	239	240	241	242	243	244	245	246	247	248	249	250	251	252	253	254	255	256	257	258	259	260	261	262	263	264	265	266	267	268	269	270	271	272	273	274	275	276	277	278	279	280	281	282	283	284	285	286	287	288	289	290	291	292	293	294	295	296	297	298	299	300	301	302	303	304	305	306	307	308	309	310	311	312	313	314	315	316	317	318	319	320	321	322	323	324	325	326	327	328	329	330	331	332	333	334	335	336	337	338	339	340	341	342	343	344	345	346	347	348	349	350	351	352	353	354	355	356	357	358	359	360	361	362	363	364	365	366	367	368	369	370	371	372	373	374	375	376	377	378	379	380	381	382	383	384	385	386	387	388	389	390	391	392	393	394	395	396	397	398	399	400	401	402	403	404	405	406	407	408	409	410	411	412	413	414	415	416	417	418	419	420	421	422	423	424	425	426	427	428	429	430	431	432	433	434	435	436	437	438	439	440	441	442	443	444	445	446	447	448	449	450	451	452	453	454	455	456	457	458	459	460	461	462	463	464	465	466	467	468	469	470	471	472	473	474	475	476	477	478	479	480	481	482	483	484	485	486	487	488	489	490	491	492	493	494	495	496	497	498	499	500	501	502	503	504	505	506	507	508	509	510	511	512	513	514	515	516	517	518	519	520	521	522	523	524	525	526	527	528	529	530	531	532	533	534	535	536	537	538	539	540	541	542	543	544	545	546	547	548	549	550	551	552	553	554	555	556	557	558	559	560	561	562	563	564	565	566	567	568	569	570	571	572	573	574	575	576	577	578	579	580	581	582	583	584	585	586	587	588	589	590	591	592	593	594	595	596	597	598	599	600	601	602	603	604	605	606	607	608	609	610	611	612	613	614	615	616	617	618	619	620	621	622	623	624	625	626	627	628	629	630	631	632	633	634	635	636	637	638	639	640	641	642	643	644	645	646	647	648	649	650	651	652	653	654	655	656	657	658	659	660	661	662	663	664	665	666	667	668	669	670	671	672	673	674	675	676	677	678	679	680	681	682	683	684	685	686	687	688	689	690	691	692	693	694	695	696	697	698	699	700	701	702	703	704	705	706	707	708	709	710	711	712	713	714	715	716	717	718	719	720	721	722	723	724	725	726	727	728	729	730	731	732	733	734	735	736	737	738	739	740	741	742	743	744	745	746	747	748	749	750	751	752	753	754	755	756	757	758	759	760	761	762	763	764	765	766	767	768	769	770	771	772	773	774	775	776	777	778	779	780	781	782	783	784	785	786	787	788	789	790	791	792	793	794	795	796	797	798	799	800	801	802	803	804	805	806	807	808	809	8010	8011	8012	8013	8014	8015	8016	8017	8018	8019	8020	8021	8022	8023	8024	8025	8026	8027	8028	8029	8030	8031	8032	8033	8034	8035	8036	8037	8038	8039	8040	8041	8042	8043	8044	8045	8046	8047	8048	8049	8050	8051	8052	8053	8054	8055	8056	8057	8058	8059	8060	8061	8062	8063	8064	8065	8066	8067	8068	8069	8070	8071	8072	8073	8074	8075	8076	8077	8078	8079	8080	8081	8082	8083	8084	8085	8086	8087	8088	8089	8090	8091	8092	8093	8094	8095	8096	8097	8098	8099	80100	80101	80102	80103	80104	80105	80106	80107	80108	80109	80110	80111	80112	80113	80114	80115	80116	80117	80118	80119	80120	80121	80122	80123	80124	80125	80126	80127	80128	80129	80130	80131	80132	80133	80134	80135	80136	80137	80138	80139	80140	80141	80142	80143	80144	80145	80146	80147	80148	80149	80150	80151	80152	80153	80154	80155	80156	80157	80158	80159	80160	80161	80162	80163	80164	80165	80166	80167	80168	80169	80170	80171	80172	80173	80174	80175	80176	80177	80178	80179	80180	80181	80182	80183	80184	80185	80186	80187	80188	80189	80190	80191	80192	80193	80194	80195	80196	80197	80198	80199	80200	80201	80202	80203	80204	80205	80206	80207	80208	80209	80210	80211	80212	80213	80214	80215	80216	80217	80218	80219	80220	80221	80222	80223	80224	80225	80226	80227	80228	80229	80230	80231	80232	80233	80234	80235	80236	80237	80238	80239	80240	80241	80242	80243	80244	80245	80246	80247	80248	80249	80250	80251	80252	80253	80254	80255	80256	80257	80258	80259	80260	80261	80262	80263	80264	80265	80266	80267	80268	80269	80270	80271	80272	80273	80274	80275	80276	80277	80278	80279	80280	80281	80282	80283	80284	80285	80286	80287	80288	80289	80290	80291	80292	80293	80294	80295	80296	80297	80298	80299	80300	80301	80302	80303	80304	80305	80306	80307	80308	80309	80310	80311	80312	80313	80314	80315	80316	80317	80318	80319	80320	80321	80322	80323	80324	80325	80326	80327	80328	80329	80330	80331	80332	80333	80334	80335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